# Analysis of the Efficiency Gaps of Wisconsin's Current Legislative District Plan and Plaintiffs' Demonstration Plan 

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## I. Introduction

My name is Kenneth Mayer and I currently am a Professor of Political Science at the University of Wisconsin-Madison, and a faculty affiliate at the Lafollette School of Public Affairs, at the University. I joined the faculty in 1989. I teach courses on American politics, the presidency, Congress, campaign finance, election law, and electoral systems.

I have been retained by counsel representing the plaintiffs in this lawsuit (the "Plaintiffs") to analyze and provide expert opinions. I have been asked to determine whether, in my opinion, it is possible to create a Wisconsin state legislative map that does not result in systemic partisan advantage, by drawing a legislative district plan that has an efficiency gap as close to zero as possible while complying with federal and state requirements at least as well as the plan enacted by the Wisconsin legislature in Act $43 .{ }^{1}$

I submit this report, which contains the opinions that I intend to give in this matter. I describe my methods for estimating the state Assembly vote in actual and hypothetical state legislative redistricting plans, and for calculating the efficiency gap for Act 43 and for the alternative demonstration plan I drew.

My opinions, which are based on the technical and specialized knowledge that I have gained from my education, training and experience, are premised on commonly used, widely accepted and reliable methods of analysis, the application of the legal requirements of redistricting, and are based on my review and analysis of the following information and materials:

- Redistricting materials available from the Wisconsin legislature at http://legis.wisconsin.gov/gis/data, including Geographic Information System (GIS)

[^0]files for Act 43 districts, and ward level election data for 2012

- Census Bureau data on population, citizenship, and location of institutionalized populations as explained below
- Election data from the 2013-2014 Wisconsin Blue Book for the 2012 State Assembly and presidential elections
- Election data from the Government Accountability Board, including ward level 2012 election results for State Assembly and presidential elections.
- GIS data, including Census population figures, block assignments, and shape files for Wisconsin, available in the GIS program Maptitude for Redistricting
- Files submitted by defendants in Baldus et al. v. Brennan et al.

I conducted my analysis using Stata, Excel, R, and Maptitude for Redistricting.

## II. Qualifications, Publications, Testimony, and Compensation

I have a Ph.D. in political science from Yale University, where my graduate training included courses in econometrics and statistics. My undergraduate degree is from the University of California, San Diego, where I majored in political science and minored in applied mathematics. My curriculum vitae is attached to this report as Exhibit 1.

All publications that I have authored and published in the past ten years appear in my curriculum vitae, attached as Exhibit 1. Those publications include the following peerreviewed journals: Journal of Politics, American Journal of Political Science, Election Law Journal, Legislative Studies Quarterly, Presidential Studies Quarterly, American Politics Research, Congress and the Presidency, Public Administration Review, and PS: Political Science and Politics. I have also published in law reviews, including the Richmond Law Review, the UCLA Pacific Basin Law Journal, and the University of Utah Law Review. My work on campaign finance has been published in Legislative Studies Quarterly, Regulation,

PS: Political Science and Politics, Richmond Law Review, the Democratic Audit of Australia, and in an edited volume on electoral competitiveness published by the Brookings Institution Press. My research on campaign finance has been cited by the Government Accountability Office, and by legislative research offices in Connecticut and Wisconsin.

My work on election administration has been published in the Election Law Journal, American Journal of Political Science, Public Administration Review, and American Politics Research. I was part of a research group retained as a consultant by the Wisconsin Government Accountability Board to review their compliance with federal mandates and reporting systems, and to survey local election officials throughout the state. I serve on the Steering Committee of the Wisconsin Elections Research Center, a unit with the UW-Madison College of Letters and Science. In 2012 I was retained by the U.S. Department of Justice to analyze data and methods regarding Florida's efforts to identify and remove claimed ineligible noncitizens from the statewide file of registered voters.

In the past eight years, I have testified as an expert witness in trial or deposition in the following cases: Baldus et al. v. Brennan et al., 849 F. Supp. 2d 840 (E.D. Wis. 2012);

Milwaukee Branch of the NAACP et al. v. Walker et al., 2014 WI 98, 357 Wis. 2d 469, 851
N.W. 2d 262; McComish et al. v. Brewer et al., No.CV- 08-1550, 2010 WL 2292213 (D.

Ariz. June 23, 2010); and Kenosha County v. City of Kenosha, No. 11-CV-1813 (Kenosha

County Circuit Court, Kenosha, WI, 2011).
I am being compensated at a rate of $\$ 300$ per hour.

## III. Opinions

## A. Summary

My opinions may be summarized as follows.

- Using a model that estimates baseline ward-level partisanship, I conclude that the redistricting plan enacted by Act 43 is significantly biased against Democrats, with an efficiency gap of $11.69 \%$. The plan achieves this via the use of classic "packing and cracking" gerrymandering techniques: concentrating Democratic voters into districts where they have overwhelming majorities (packing), and drawing other districts so that Democrats constitute partisan minorities well below $50 \%$ and unlikely to win legislative seats (cracking). In doing so, Republicans guarantee a strong majority of legislative seats, even if they obtain well below $50 \%$ of the statewide legislative vote. In 2012, Republicans won $61 \%$ of State Assembly seats ( 60 of 99 ) while achieving only $46.5 \%$ of the statewide vote (as measured by the presidential vote, a common proxy for statewide partisanship).
- Using the same measure of partisan strength that the Wisconsin state legislature used in assessing partisan impact of proposed districts in Act 43, Act 43 has an efficiency gap of $12.36 \%$.
- I created a demonstration redistricting plan (the "Demonstration Plan") that is equivalent to Act 43 on population deviation, has fewer political subdivision splits, and has better compactness scores, with a much lower efficiency gap score of $2.20 \%$. This is less than one-fifth of the Act 43 efficiency gap.
- The Demonstration Plan shows that the partisan advantage secured in Act 43 was in no sense required in order to adhere to the constitutional and statutory requirements of legislative redistricting.


## B. Measuring Partisanship in Actual and Hypothetical Districting Plans

The efficiency gap is a measure of "wasted votes" that fall into two categories: those votes cast for a losing candidate in a district (lost votes), and votes cast for the winning candidate above what is necessary to win (surplus votes). In an existing set of districts, the calculation is based on the actual vote in each district, with adjustments for uncontested races (Stephanopoulos and McGhee 2015). Larger imbalances in the number of wasted votes signify a degree of partisan unfairness against the political party with more wasted votes.

Calculating the efficiency gap in the Demonstration Plan requires estimating what the underlying partisan vote would be in each newly drawn (and hypothetical) district. The gap cannot be estimated by simply rearranging the votes cast in actual Assembly contests into a new
district configuration, as the votes cast for specific Assembly candidates in each district are a function of the electoral environment in that district and whether a race is even contested by both parties. A large literature has developed around the problem of estimating the likely election results in redistricting plan alternatives and calculating summary statistics that characterize existing and hypothetical plans (Gelman and King 1994; Cain 1985).

In most applications, the partisan consequences of a redistricting plan are expressed in terms of the effect on future elections: using prior election results to predict outcomes in subsequent election cycles, or estimating the statewide vote swing required to significantly change the partisan composition of the legislature from one election to the next (Gelman and King 1990; Cain 1985). The results are typically expressed as the estimated two-party vote percentages in each new district (Gelman and King 1994), which are sufficient to forecast who will win an election and calculate swing ratios and seats-votes curves. ${ }^{2}$

My aim is different. Instead of estimating future election results for an existing or proposed hypothetical plan, my goal was to determine whether it was possible to draw a district plan following the 2010 Census that minimized the efficiency gap while maintaining strict fidelity to the federal and state constitutional requirements of population equality, contiguity, compactness, respect for political subdivisions, and compliance with the Voting Rights Act. The efficiency gap is a function of the number of wasted votes, and therefore requires a model that generates predictions of how many votes would have been cast for Democratic and Republican candidates in 2012 in a different district configuration, rather than simply vote

[^1]percentages. My methods provide a way of estimating what the 2012 Assembly election results would have been in such a Demonstration Plan.

Given appropriate data, it is possible to generate reliable and accurate vote count predictions that can be aggregated to any district boundaries. What is required is a set of independent variables that accurately predict the vote in state Assembly elections but which are to the greatest extent possible exogenous to that vote, meaning that the independent variables have underlying values that do not themselves depend on the district vote. If this condition is met, we can estimate what the district vote would have been in an alternative district configuration, since the independent variables do not depend on any particular district configuration. This is not an issue in models that predict future election results, since by definition variables measured today are exogenous to outcomes that occur several years in the future. Because I use one set of election results (the 2012 presidential vote) as part of a model that predicts another set of contemporaneous election results (the 2012 Assembly vote), it is an important but manageable methodological issue.

My method consists of two steps. The first is the construction of a regression model that predicts the 2012 Assembly vote as a function of partisanship, population, demographics, incumbency, and fixed geographic boundaries in Wisconsin's roughly 6,600 wards. In doing so, I establish the empirical relationships between a set of exogenous variables independent of any specific district configurations and the actual Assembly vote in existing wards. In the second step, I use this model to generate a forecast of Assembly vote preferences as a function of these independent variables, and disaggregate this forecast to the Census block level. Using these block level estimates of the Assembly vote, I draw a Demonstration Plan and estimate the Assembly vote and efficiency gap in the resulting districts.

## 1. Step One: A Model of Voting in Assembly Elections

Estimating the Assembly vote in alternative district configurations requires a model that can generate accurate estimates of the underlying partisanship of a district. As I noted above, the most common models regress the observed Assembly vote on measures of district partisan preferences and other variables known to affect the vote, and generate a predicted value of the vote based on the values of the independent variables. Changing district boundaries will change the values of the independent variables as new voters are moved into the district and others moved out, which in turn allows forecasts of what the vote would be in those new districts.

What I am interested in estimating is how many votes will be cast for Democratic and Republican candidates in each district in a demonstration district plan. This involves a different set of variables than is typical in models that evaluate the percentage of votes each party receives, since I require a measure that accounts for both differences in ward populations and variation in turnout.

I use ward level vote totals as the unit of analysis to increase the number of observations available and allow for more precise estimates. Wisconsin's 99 Assembly districts are composed of roughly 6,600 wards, with districts containing between 24 and 153 wards. While the ideal population of an Assembly district is 57,444 , wards have an average population of approximately 869 people, and are far more demographically homogeneous. ${ }^{3}$

[^2]There are four reasons analysis at the ward level is preferable to analysis at the district level. The first is a matter of sheer numbers: the precision of coefficient estimates, forecasting accuracy, and overall statistical power are all strongly related to the number of observations (or sample size). An $n$ of 6,600 is far preferable to an $n$ of 99 , all other things being equal. ${ }^{4}$

The second is the amount of information lost when smaller units are ignored. From a statistical standpoint, using district data when ward data are available imposes the assumption that the values of all of the ward-level variables are equal to the district level variables, when we know this to be untrue immediately upon inspection. Assembly district 1, for example, has 110 populated wards, ranging in population between one and 999 people. In 2012, 73.4\% of the voting age population cast ballots in the Assembly contest, and the victorious Republican Assembly candidate received $51.3 \%$ of the vote. At the ward level, however, there was considerable variation, with the Republican vote percentage ranging from a low of $38.4 \%$ to a high of $75 \%$, and turnout ranging from $50 \%$ to over $90 \%$. Ignoring this information and variation will lead to less accurate estimates and forecasts.

Third, in the second step of the analysis I disaggregate ward level estimates to the block level. Minimizing the differences in size and maximizing the homogeneity across that disaggregation will lead to more accurate block level estimates.

And fourth, each Census block is assigned to a single ward, ${ }^{5}$ with a unique numerical code that identifies the block's location. ${ }^{6}$ These codes allow for disaggregating ward level data

[^3]into blocks and generating inputs for the redistricting software I use in the second step of my analysis.

I use two main sources of data. The first is redistricting data prepared by the Wisconsin Legislative Technology Services Bureau (LTSB), which consists of spreadsheets with ward level Census population data and election results, as well as ward and district shape files containing this data that can be imported into GIS software. ${ }^{7}$ The second source is official election results published by the Government Accountability Board (GAB), both online and in the 2013 edition of the Wisconsin Blue Book.

In my experience working with large data sets, and especially when dealing with complex GIS data, I have found data errors to be a common problem. I assessed the reliability of the LTSB data by checking it against the GAB election data, and found numerous errors that required correction, as well some errors that could not be corrected. ${ }^{8}$ I describe these errors and my corrections in greater detail in an annex to this report. All subsequent references to ward level vote or population counts uses these corrected vote totals.

The regression model used to predict Assembly vote totals takes the standard form of

$$
\mathrm{Y}_{i}=\alpha+\beta \mathrm{X}_{i}+\varepsilon_{i},
$$

where $\mathrm{Y}_{i}$ is the dependent variable in ward $i, \mathrm{X}_{i}$ is a set of independent variables in ward $i$, and $\alpha$, $\beta$, and $\varepsilon_{i}$ are parameters estimated as a function of the variables. The full model is:

$$
\begin{aligned}
& \text { Assembly } \\
& \text { Vote }_{i}
\end{aligned}=\alpha+\beta_{1} \text { Total VEP }_{i}+\beta_{2} \text { Black VEP }_{i}+\beta_{3}{\text { Hispanic } V E P_{i}}^{\text {A }}
$$

[^4]\[

$$
\begin{gathered}
+\beta_{4} \begin{array}{c}
\text { Democratic } \\
\text { Presidential Vote }_{i}
\end{array}+\beta_{5} \begin{array}{c}
\text { Republican } \\
\text { Presidential Vote }_{i}
\end{array} \\
+\beta_{6} \text { Democratic }_{\text {Incumbent }_{i}}+\beta_{7}^{\text {Republican }_{\text {Incumbent }_{i}}^{\text {Res }}+\sum_{j=1}^{71} \gamma_{j} \text { County }_{j}+\varepsilon_{i}}
\end{gathered}
$$
\]

Where

Assembly Vote

Black VEP Voting eligible Black population in ward $i$

Hispanic VEP Voting eligible Hispanic population in ward $i$

Democratic Number of votes cast for Barack Obama in the 2012
Presidential Vote

Republican Number of votes cast for Mitt Romney in the 2012
Presidential Vote
Democratic
Incumbent

Republican $\quad 1$ if the Assembly election in ward $i$ has a Republican Incumbent

County candidate in the 2012 Assembly election in ward $i$. I estimate separate equations for the Democratic and Republican candidates

Total VEP $\quad$ Voting eligible population in ward $i$, as measured in the 2010 Census presidential election in ward $i$ presidential election in ward $i$

Number of votes cast for the Republican or Democratic

The model explains the Assembly vote as a function of four types of variables: district demographics, underlying partisanship, incumbency, and fixed geographic effects.

[^5]
## a. The Dependent Variable: Ward level Assembly Vote

The key quantity of interest in this analysis is the number of Assembly votes for each party, and it is the dependent variable in the model, using LTSB ward data that I corrected using the process outlined above. Since I am interested in estimating actual vote counts and not the percentage of the two party vote, I estimate separate equations for votes received by each party. ${ }^{10}$ Estimating vote counts provides more accuracy than vote percentages, as it controls for variations in turnout across districts. ${ }^{11}$

## b. Independent Variables: Demographic Data

The first three independent variables - Total Voting Age Population (VEP), Black VEP,
and Hispanic VEP - are the 2010 Census voting age population counts by ward, adjusted to remove ineligible voters. ${ }^{12}$ Total VEP constitutes a baseline of the size of the voting population, reflecting the fact that the number of votes will be a function of total population. Black and Hispanic VEP are additional controls that reflect the partisan tendencies of key subpopulations as

[^6]well as turnout likelihood. Traditionally, both African American and Hispanic populations vote at lower rates that whites, although in 2012 African American turnout was comparable to white turnout. Hispanic populations vote at lower rates than other demographic groups, in part because of a higher noncitizen population, but also because of socioeconomic factors known to reduce turnout.

I expect weak relationships for these measures because of the importance of the next set of variables, which reflect actual voting in the 2012 presidential election.

## c. Independent Variables: Measures of Partisanship

The next two variables are the number of votes cast for the Democratic and Republican candidates for president in the 2012 election. The presidential vote is widely used as an exogenous measure of district level partisanship (Ansolabehere, Snyder and Stewart 2000, 2001; Gelman and King 1994; Glazier, Grofman, and Robbins 1987; McDonald 2014; Jacobson 2003, 2009), and it correlates very strongly with other more complex measures of partisan strength (Levendusky, Pope, and Jackman 2008).

The presidential vote is, not surprisingly, an extremely strong predictor of the legislative vote. If we know how many votes were cast for the Republican presidential candidate in a ward we will have a very good idea, subject to some conditions, of how many votes will be cast for the Republican candidate in the legislative election in that ward. While not everyone who votes for the Republican presidential candidate will vote for the Republican state legislative candidate, nearly all will, and we can precisely quantify the nature of that relationship.

The strength of the relationship between presidential and Assembly votes is clear in Figures 1 through 3, which plot the total Assembly vote, Republican Assembly vote, and Democratic Assembly vote in 2012 by the respective presidential vote in each contested ward (where voters have an opportunity to express a preference for either party in the legislative race).



Figure 3: Presidential Vote and Assembly Vote 2012


Figure 1 shows that the number of presidential votes cast in a ward is very strongly related to the number of Assembly votes, although almost all wards show a "roll off" as some presidential voters opt not to mark the ballot in the assembly race (the reference line shows where the number of presidential and Assembly votes would be equal). Such drop-offs are ubiquitous in down-ticket races, because voters have less information about lower-level candidates and often have weaker or nonexistent preferences (Wattenberg, McAllister, and Salvanto 2000).

The graphs for the Republican (Figure 2) and Democratic (Figure 3) votes show more variance around this reference line, indicating that some voters are splitting their tickets by voting for a presidential candidate of one party and an Assembly candidate of the other. Nevertheless, the relationship between the number the Republican and Democratic presidential and Assembly votes is apparent. Taken together, these figures indicate that the presidential vote is a very strong predictor of the Assembly vote.

An important property of the presidential vote as an independent variable in this model is that it can be treated as exogenous to (i.e., not caused by) the legislative vote. Exogeneity can be described in two ways. The first is in causal terms. Most voters will vote for the same party for the president and state Assembly, as the above graphs show. These voters are consistent because they are Democrats or Republicans, and partisanship is the factor that explains both vote choices. Other voters will make their Assembly choice based on their presidential vote, because they use party labels as a cue when voting in a down-ticket race. "[P]arties are generally known by the presidential candidates they nominate, and candidates for state legislative races are a good deal less well known to voters than the congressional candidates who ride presidential coattails" (Campbell 1986, 46). Few voters, if any at all, will decide on an Assembly candidate first and
then vote for president on the basis of their Assembly vote preference. The causal arrow runs from the presidential vote to the Assembly vote, not from the Assembly vote to the presidential vote. This is why we speak of presidential coattails affecting legislative races, and not the other way around (Campbell 1986; Jacobson 2009).

The second reason why the presidential vote is exogenous to the Assembly vote is that it is not affected by local district-level conditions such as incumbency, spending, or candidate quality (Abramowitz, Alexander, and Gunning 2006, 87). The broader factors that influence the presidential vote, and the presidential candidates themselves, are the same in every Assembly district. The presidential vote is affected by underlying partisanship, national conditions and the characteristics of the presidential candidates, factors that are constant whether that vote is aggregated at the state, district, or ward levels.

To put it another way, a change in the statewide presidential vote is virtually certain to affect state legislative election results. Adding or subtracting hundreds of thousands of Democrats or Republicans will alter voting patterns at the district level. However, nobody would expect that the statewide presidential result will be affected by the configuration of legislative districts. The statewide presidential vote would be the same, no matter how the district lines are drawn. Consequently, we can consider the presidential vote as exogenous to, but a causal factor of, the state legislative vote.

## d. Independent Variables: Incumbency

The incumbency advantage is perhaps the most well-known feature of contemporary legislative elections (Jacobson 2009, 30-35). Legislative incumbents rarely lose, and usually win by large margins. All other things being equal, an incumbent will get more votes than a non-
incumbent. The causes of this advantage are less important in this context than its magnitude. ${ }^{13}$ The model takes into account the incumbency advantage by noting whether an incumbent is running in an Assembly district.

Incumbency effects are measured with a dummy variable equal to 1 when a candidate is an incumbent, and 0 otherwise, ${ }^{14}$ multiplied by the ward voting eligible population to create an interactive variable that accounts for differences in size from one ward to the next. Since the dependent variable is an actual vote count, the value of incumbency - in terms of how many additional votes incumbents receive - will vary with the number of voters who reside in a ward.

## e. Independent Variables: County Effects

The last set of variables estimate the effect that county geography has on the Assembly vote. Some counties in Wisconsin are heavily Republican (Ozaukee, Washington, Waukesha) and some heavily Democratic (Dane, Douglas, Milwaukee). It is possible that a voters' county of residence could have an effect on the vote choice, whether because of sorting, socialization or assimilation, or other unobserved effects. Including dummy variables for each county will capture these effects if they exist. There are 71 county variables (excluding Dunn County) set to 1 when a ward is located in that county, 0 otherwise.

[^7]
## f. Estimation and Results

Using Stata IC 11.2 I performed ordinary least squares regression, using 2012 ward data from contested districts where both Republican and Democratic candidates were on the ballot. ${ }^{15}$ Analyzing contested races solves the problem of trying to estimate partisan support in a district where voters have no opportunity to express their support for one side (Gelman and King 1994). The fact that Republicans registered 0 Assembly votes in the $78^{\text {th }}$ district (Madison), and Democrats 0 votes in the $58^{\text {th }}$ district (Washington County), does not mean there are no Republicans in the $78^{\text {th }}$ or Democrats in the $58^{\text {th }}$ districts, or that a Republican or Democratic candidate would receive zero votes if one were on the ballot. Using uncontested races in this initial analysis would produce inaccurate estimates of party strength in those districts.

The results for the Democratic and Republic regression models appear in Table 1. ${ }^{16}$ Most variables show the expected effects, particularly the very strong impact of the presidential vote. The $r^{2}$ values are extremely high, and the standard errors of the regression models (Root MSE) are low. The model is also extremely accurate: when compared to actual ward vote, the model's predictions of the Republican ward totals are within 16 votes, and the Democratic predictions are within 18 votes.

Figure 4 shows the overall accuracy of the model by plotting the predicted ward level vote totals by the actual vote totals in each ward. Predictions for both Democrats and

[^8]Republicans are grouped tightly around the 45-degree line where predicted and actual values would be equal.

Figure 5 shows the accuracy of the model at the district level, which is the more relevant quantity for real-world applicability. I calculated district level results by aggregating wards into the associated Assembly district, using LTSB assignments. The district-level estimates are very close to the actual vote totals, and the average absolute error is 356 votes for Democratic candidates and 344 votes for Republican candidates.

Table 1
Regression Results: 2012 Assembly Votes, Contested Districts County fixed effect variables not shown,

| Dependent Variable | Independent Variable |  |
| :---: | :---: | :---: |
|  | Assembly Republican Votes | Assembly Democratic Votes |
| Total Voting Eligible Population | $\begin{gathered} 0.009 \\ (.0070) \end{gathered}$ | $\begin{aligned} & -0.008 \\ & (.0122) \end{aligned}$ |
| Black Voting <br> Eligible <br> Population | $\begin{aligned} & -0.026 \\ & (.0215) \end{aligned}$ | $\begin{aligned} & -0.021 \\ & (.044) \end{aligned}$ |
| Hispanic Voting eligible <br> Population | $\begin{aligned} & -0.0083 \\ & (.0321) \end{aligned}$ | $\begin{gathered} -0.149^{* *} \\ (.05) \end{gathered}$ |
| Democratic <br> Presidential Votes | $\begin{aligned} & 0.0072 \\ & (.0173) \end{aligned}$ | $\begin{gathered} 0.931^{* * *} \\ (.028) \end{gathered}$ |
| Republican <br> Presidential <br> Votes | $\begin{gathered} 0.946 * * * \\ (.0086) \end{gathered}$ | $\begin{aligned} & 0.013 \\ & (.013) \end{aligned}$ |
| Democratic Assembly Incumbent | $\begin{gathered} -0.021^{* * *} \\ (.006) \end{gathered}$ | $\begin{gathered} 0.028^{* *} \\ (.007) \end{gathered}$ |
| Republican <br> Assembly <br> Incumbent | $\begin{aligned} & 0.011^{* *} \\ & (.0042) \end{aligned}$ | $\begin{gathered} -0.014 * * \\ (.005) \end{gathered}$ |
| Constant | $\begin{gathered} -0.92 \\ (7.52) \end{gathered}$ | $\begin{gathered} 9.8 \\ (5.4) \end{gathered}$ |
| $N$ | 5,282 | 5,282 |
| $r^{2}$ | . 9903 | . 9843 |
| Root MS Error | 15.8 | 17.7 |
| Robust standard errors clustered by Assembly District in parentheses. <br> ${ }^{*} \mathrm{p}<.05,{ }^{* *} \mathrm{p}<0.01,{ }^{* * *} \mathrm{p}<0.001$ |  |  |

Figure 4: Ward Level Predicted vs. Actual Assembly Vote - 2012


Figure 5: Predicted vs. Actual District Assembly Vote - 2012
Both Parties, Contested Districts


As important as the prediction of actual district vote totals is the model's ability to accurately identify the winner, as the efficiency gap calculation is sensitive to the party of the winners and losers. ${ }^{17}$ The accuracy of the model is shown in Table 2, which gives the actual and predicted vote percentages of the two-party vote for Republican candidates in contested districts. ${ }^{18}$

[^9]Table 2 - Predicted vs. Actual Vote Percentages,
Contested Districts

|  |  |  |  |  |
| :---: | :---: | :---: | :---: | ---: |
| Assembly |  |  |  |  |
| District |  |  |  |  | | Actual |
| :---: |
| GOP Vote |
| $\%$ | | Predicted |
| :---: |
| GOP Vote |
| $\%$ | | Correct |
| :---: |
| Winner? |$\quad$ Error


| 67 | $53.3 \%$ | $53.5 \%$ | $Y$ | $0.2 \%$ |
| :--- | :--- | :--- | :--- | ---: |
| 68 | $52.4 \%$ | $50.7 \%$ | $Y$ | $-1.8 \%$ |
| 69 | $61.2 \%$ | $58.5 \%$ | $Y$ | $-2.7 \%$ |
| 70 | $49.7 \%$ | $50.1 \%$ | N | $0.4 \%$ |
| 71 | $39.0 \%$ | $39.3 \%$ | $Y$ | $0.2 \%$ |
| 72 | $50.2 \%$ | $51.3 \%$ | $Y$ | $1.1 \%$ |
| 74 | $41.0 \%$ | $41.1 \%$ | $Y$ | $0.1 \%$ |
| 75 | $48.9 \%$ | $49.2 \%$ | $Y$ | $0.2 \%$ |
| 80 | $36.1 \%$ | $35.3 \%$ | $Y$ | $-0.8 \%$ |
| 81 | $38.1 \%$ | $39.6 \%$ | $Y$ | $1.4 \%$ |
| 82 | $60.3 \%$ | $61.6 \%$ | $Y$ | $1.4 \%$ |
| 83 | $69.8 \%$ | $71.6 \%$ | $Y$ | $1.9 \%$ |
| 84 | $62.8 \%$ | $61.8 \%$ | $Y$ | $-1.0 \%$ |
| 85 | $48.2 \%$ | $48.7 \%$ | $Y$ | $0.5 \%$ |
| 86 | $55.7 \%$ | $56.1 \%$ | $Y$ | $0.4 \%$ |
| 87 | $58.6 \%$ | $58.3 \%$ | $Y$ | $-0.3 \%$ |
| 88 | $52.5 \%$ | $54.1 \%$ | $Y$ | $1.7 \%$ |
| 89 | $59.1 \%$ | $59.2 \%$ | $Y$ | $0.1 \%$ |
| 90 | $39.6 \%$ | $37.7 \%$ | $Y$ | $-1.9 \%$ |
| 93 | $50.8 \%$ | $52.0 \%$ | $Y$ | $1.2 \%$ |
| 94 | $39.4 \%$ | $39.4 \%$ | $Y$ | $0.0 \%$ |
| 96 | $59.6 \%$ | $59.7 \%$ | $Y$ | $0.1 \%$ |
| 97 | $64.7 \%$ | $64.4 \%$ | $Y$ | $-0.3 \%$ |
| 98 | $70.5 \%$ | $70.0 \%$ | $Y$ | $-0.5 \%$ |
| 99 | $76.3 \%$ | $77.0 \%$ | $Y$ | $0.7 \%$ |

The regression model identifies the correct winner in 70 of 72 districts ( $97.2 \%$ ); that is, it accurately identifies the candidate who received the most votes. In the two misclassified races, the Republican candidates received $51.9 \%$ and $49.7 \%$ of the vote. The average absolute error in the vote margin is $1.49 \%$.

## g. Out of Sample Forecasting Accuracy

These results, which compare predicted election results to the actual election results, demonstrate that the model is very accurate. A harder test involves the accuracy of predictions using data not in the sample - that is, applying the model to data and election results that are different from the data used to estimate the model. To test the model's out of sample accuracy, I reran the model 72 times (once for every contested district) excluding every ward in one single
contested district each time, ${ }^{19}$ and then used the results of that estimation to predict the vote totals in wards in the excluded district using the independent variable values for those wards. For example, in the first run I excluded all wards in Assembly district 2 (see footnote 20), and estimated the model using data from the other seventy one contested districts. I then used the results to predict the vote totals in the 2 nd district, and compared the prediction to the actual vote totals. Since we know the actual election results in excluded districts, this exercise is a "hard test" of the model's general predictive ability.

Figure 6 and Table 3 show the results for the 60 contested districts in which the full model could be estimated. ${ }^{20}$ The average district forecast error of the Republican vote percentage increased slightly, to $2.1 \%$, but the out of sample forecasts identified the correct winner in 59 out of 60 races ( $98.3 \%$ ). In Figure 6, which plots the actual versus predicted vote totals, the points are not grouped as tightly around the 45-degree line as they are in the full model predictions (Figure 5), but still show a very high degree of accuracy.

Table 3 -Out of Sample Predicted vs. Actual Vote
Percentages, Contested Districts

| Assembly <br> District | Actual <br> GOP Vote <br> $\%$ | Predicted <br> GOP Vote <br> $\%$ | Correct <br> Winner? | Error |
| :---: | :---: | :---: | :---: | :---: |
| 2 | $58.7 \%$ | $59.0 \%$ | $Y$ | $0.3 \%$ |
| 3 | $60.4 \%$ | $57.5 \%$ | $Y$ | $-2.9 \%$ |
| 4 | $55.7 \%$ | $54.3 \%$ | $Y$ | $-1.3 \%$ |
| 5 | $55.9 \%$ | $58.9 \%$ | $Y$ | $2.9 \%$ |
| 13 | $60.6 \%$ | $60.4 \%$ | $Y$ | $-0.2 \%$ |

[^10]| 14 | 59.1\% | 61.0\% | Y | 1.8\% |
| :---: | :---: | :---: | :---: | :---: |
| 15 | 58.3\% | 56.7\% | Y | -1.6\% |
| 20 | 42.4\% | 39.9\% | Y | -2.5\% |
| 21 | 59.3\% | 56.3\% | $Y$ | -3.1\% |
| 23 | 62.3\% | 61.4\% | Y | -0.9\% |
| 24 | 62.4\% | 60.2\% | $Y$ | -2.3\% |
| 25 | 57.7\% | 55.7\% | Y | -2.0\% |
| 26 | 51.3\% | 58.6\% | Y | 7.3\% |
| 27 | 57.8\% | 50.3\% | Y | -7.5\% |
| 28 | 56.2\% | 55.1\% | $Y$ | -1.2\% |
| 29 | 55.9\% | 54.6\% | Y | -1.3\% |
| 30 | 55.8\% | 57.2\% | $Y$ | 1.4\% |
| 31 | 56.5\% | 55.7\% | Y | -0.9\% |
| 32 | 59.1\% | 60.2\% | Y | 1.1\% |
| 33 | 64.9\% | 63.0\% | Y | -1.9\% |
| 37 | 54.3\% | 56.3\% | Y | 2.0\% |
| 38 | 60.0\% | 62.3\% | Y | 2.3\% |
| 39 | 60.4\% | 59.0\% | Y | -1.5\% |
| 41 | 58.0\% | 56.2\% | Y | -1.7\% |
| 42 | 56.6\% | 51.8\% | $Y$ | -4.8\% |
| 43 | 42.3\% | 43.3\% | $Y$ | 1.1\% |
| 44 | 38.4\% | 40.8\% | Y | 2.5\% |
| 45 | 36.1\% | 34.1\% | Y | -2.0\% |
| 46 | 35.2\% | 34.1\% | Y | -1.0\% |
| 47 | 29.0\% | 30.9\% | $Y$ | 1.8\% |
| 50 | 51.7\% | 53.1\% | Y | 1.4\% |
| 51 | 51.9\% | 48.7\% | N | -3.2\% |
| 52 | 60.7\% | 59.4\% | Y | -1.3\% |
| 53 | 60.1\% | 64.4\% | $Y$ | 4.4\% |
| 54 | 39.8\% | 43.8\% | $Y$ | 4.0\% |
| 55 | 65.2\% | 56.0\% | $Y$ | -9.3\% |
| 56 | 58.3\% | 59.9\% | $Y$ | 1.6\% |
| 60 | 71.2\% | 73.9\% | $Y$ | 2.8\% |
| 61 | 55.7\% | 54.9\% | $Y$ | -0.8\% |
| 62 | 53.1\% | 54.5\% | $Y$ | 1.4\% |
| 63 | 58.4\% | 57.1\% | $Y$ | -1.3\% |
| 67 | 53.3\% | 54.7\% | $Y$ | 1.4\% |
| 69 | 61.2\% | 57.2\% | $Y$ | -4.0\% |
| 70 | 49.7\% | 49.7\% | $Y$ | 0.0\% |
| 71 | 39.0\% | 40.1\% | $Y$ | 1.1\% |
| 72 | 50.2\% | 53.0\% | $Y$ | 2.8\% |
| 80 | 36.1\% | 35.1\% | $Y$ | -1.0\% |
| 81 | 38.1\% | 40.8\% | Y | 2.6\% |


| 82 | $60.3 \%$ | $62.0 \%$ | $Y$ | $1.8 \%$ |
| :--- | :--- | :--- | :--- | :--- |
| 83 | $69.8 \%$ | $71.8 \%$ | $Y$ | $2.0 \%$ |
| 84 | $62.8 \%$ | $61.7 \%$ | $Y$ | $-1.1 \%$ |
| 85 | $48.2 \%$ | $49.0 \%$ | $Y$ | $0.8 \%$ |
| 86 | $55.7 \%$ | $56.9 \%$ | $Y$ | $1.2 \%$ |
| 87 | $58.6 \%$ | $54.6 \%$ | $Y$ | $-3.9 \%$ |
| 88 | $52.5 \%$ | $54.6 \%$ | $Y$ | $2.1 \%$ |
| 89 | $59.1 \%$ | $59.0 \%$ | $Y$ | $-0.1 \%$ |
| 90 | $39.6 \%$ | $36.9 \%$ | $Y$ | $-2.7 \%$ |
| 97 | $64.7 \%$ | $64.2 \%$ | $Y$ | $-0.5 \%$ |
| 98 | $70.5 \%$ | $69.9 \%$ | $Y$ | $-0.5 \%$ |
| 99 | $76.3 \%$ | $77.3 \%$ | $Y$ | $1.0 \%$ |



The model does an excellent job accurately forecasting vote totals and election results, and provides a solid foundation for estimating hypothetical vote totals in an alternative district plan.

## h. Comparison to 2011 Republican Expert Baseline Partisanship Measure

The method I have outlined here is a standard technique in the analysis of redistricting plans: creating a baseline measure of partisanship that is independent of a particular district configuration, and applying those estimates to alternative hypothetical district plans.

Indeed, in preparing the district plan that would become Act 43, the state legislature went through the same analytical exercise, generating partisanship measures to forecast what the election results would be in the districts enacted in that plan. The expert that the legislative Republicans relied on to conduct that analysis, Dr. Ronald Keith Gaddie, described the process and method as "an effort to create a partisan normal vote measure or a partisan baselining measure to use to apply to different districts to ascertain their political tendency.,21 The results of his regression analysis of the districts in Act 43 are in a spreadsheet used to evaluate the plan entitled "Final Map" which contains open seat baseline partisan estimates for existing and new Assembly districts.

Figure 7 compares Dr. Gaddie's open-seat baseline partisanship measure for the Act 43 districts with the equivalent results of my model, excluding the $8^{\text {th }}$ and $9^{\text {th }}$ Assembly districts which were redrawn by the Federal Court and are therefore not comparable. Gaddie's partisan baseline measure is plotted on the x -axis, and my measure on the y -axis. My measure is the expected partisan performance in actual Act 43 districts, with incumbency effects removed. ${ }^{22}$ The two measures are strongly related, indicating that both are capturing stable features of partisanship in Wisconsin. The line is a bivariate regression line produced by using Dr. Gaddie's partisanship estimate as the independent variable and my measure as the dependent variable.

[^11]The r-squared for this regression is 0.96 , indicating that the two measures are almost perfectly related, and are both capturing the same underlying partisanship.

The most important characteristics of Gaddie's measure is that it constitutes a true forecast of what was expected to occur in the 2012 elections, since the measure itself was generated in 2011 using data from the 2004-2010 elections. As I show below, this metric can be used to generate an efficiency gap measure of what was likely to happen (indeed, what did happen) in the 2012 election.


## 2. Step Two - Predicting Votes in a Demonstration District Plan

## a. Creating a Demonstration District Plan

With the model parameters in hand, I can estimate baseline partisanship and vote totals in every ward, including those uncontested by both parties (because I have independent variables in all wards, even when only one party is on the Assembly ballot). For uncontested districts, the predicted ward vote totals are what would be expected if both parties ran a candidate, based on the values of the independent variables in the wards. I then use these predicted ward level vote totals to generate vote estimates at the Census block level, and build a demonstration district using Census blocks as my basic unit. Because the variables used in the model are exogenous to district configuration and the out of sample predictions are accurate, the results of the analysis in Step one represent a valid measure of what the Assembly vote would have been in a different district configuration.

I calculated estimated "open seat" vote totals, by subtracting the incumbency advantage in every district in which an incumbent ran. This is a more accurate method of determining the baseline partisanship of a district, as it removes the effect of incumbents, who may or may not be running in an alternative plan. This baseline process is standard in the discipline, and was used by the expert retained by the state legislature, Dr. Ronald Keith Gaddie, to analyze the partisan effects of Act 43 during the redistricting process.

To obtain block level vote estimates, I disaggregated the ward level predicted values for the Democratic and Republican vote totals to individual blocks in that ward, based on each block's share of the ward vote eligible population. This technique is widely used and accepted in the discipline (McDonald 2014; Pavia. and López-Quílez 2013). Census blocks have a voting eligible population range between 0 and 2,988, with an average of approximately 17 people. Wards contain an average of 40 blocks, although the range is substantial, with a minimum of 1
and a maximum of 740. At the end of this disaggregation process, I have a predicted Democratic and Republican Assembly vote total for each Census block in the state.

Table 4 shows an illustrative example, using Ward 23 in the city of Waukesha. This ward, located in the southeastern part of the city, had a 2010 Census population of 1,426, a voting age population of 1,089 , and a voting eligible population of 1,071 . The voting model generated estimates of 552 Republican and 318 Democratic votes in an open seat Assembly race in that ward. The ward contains twenty five Census blocks ranging in population from 0 to 127 , with a voting eligible population range of 0 to 115 .

The first column in Table 4 is the block's geographic identifier, a unique code. ${ }^{23}$ The next column is the block's voting eligible population (VEP) calculated as described in the previous section by removing noncitizens and institutionalized persons (although there are no prisons in this ward). The third column is the block's share of the ward's total VEP of 1,071 ; for the first block in the table it is $38 \div 1,071=.0352$, or $3.52 \%$. The next column is block level Republican vote estimate, calculated as $3.52 \%$ the ward Republican vote of 552 , or 19.438. While the table rounds these vote totals, I use fractional values in the actual calculations.

[^12]Table 4 - Ward to Block Disaggregation
City of Waukesha Ward 23

| Ward Voting Eligible Population |  |  |  | 1,071 |
| :---: | :---: | :---: | :---: | :---: |
| Ward Estimated Republican Assembly Vote |  |  |  | 552 |
| Ward Estimated Democratic Assembly Vote |  |  |  | 318 |
| Block Geographic Identifier | Block VEP | Block Share of Ward VEP <br> (Block VEP $\div 1,071$ ) | Block Level Republican Vote Estimate <br> (Block Share * 522) | Block Level Democratic Vote Estimate <br> (Block Share * 318) |
| 551332024001002 | 38 | 3.52\% | 19 | 11 |
| 551332024001003 | 56 | 5.24\% | 29 | 17 |
| 551332024001004 | 65 | 6.06\% | 33 | 19 |
| 551332024001005 | 30 | 2.77\% | 15 | 9 |
| 551332024001007 | 47 | 4.37\% | 24 | 14 |
| 551332024001008 | 81 | 7.57\% | 42 | 24 |
| 551332024001009 | 12 | 1.11\% | 6 | 4 |
| 551332024001010 | 50 | 4.70\% | 26 | 15 |
| 551332024001011 | 26 | 2.46\% | 14 | 8 |
| 551332024001012 | 25 | 2.32\% | 13 | 7 |
| 551332024001013 | 44 | 4.14\% | 23 | 13 |
| 551332024001014 | 60 | 5.57\% | 31 | 18 |
| 551332024001015 | 30 | 2.77\% | 15 | 9 |
| 551332024001016 | 53 | 4.99\% | 28 | 16 |
| 551332024001017 | 0 | 0.00\% | 0 | 0 |
| 551332024002009 | 10 | 0.93\% | 5 | 3 |
| 551332024002010 | 50 | 4.68\% | 26 | 15 |
| 551332024002011 | 65 | 6.06\% | 33 | 19 |
| 551332024002012 | 37 | 3.44\% | 19 | 11 |
| 551332024002013 | 39 | 3.61\% | 20 | 12 |
| 551332024003036 | 41 | 3.78\% | 21 | 12 |
| 551332024003039 | 15 | 1.39\% | 8 | 4 |
| 551332024003040 | 62 | 5.76\% | 32 | 18 |
| 551332024003042 | 22 | 2.01\% | 11 | 6 |
| 551332025005011 | 115 | 10.73\% | 59 | 34 |

Next, I input this block level data into a commercial GIS software package used for redistricting (Maptitude for Redistricting 2013, Build 2060) matching each block in the database of estimated votes with the same block in the Maptitude data using the block identification code.

Finally, I drew a redistricting plan with the goal of minimizing the efficiency gap while adhering to the Wisconsin and federal Constitutional requirements of equal population, contiguity, compactness, and respect for political subdivisions. Beyond these criteria. the primary decision rule was creating competitive districts where possible, and balancing the number of districts with large Democratic and Republican majorities.

Figures 8 and 9 show the statewide map and the districts in the Milwaukee area.

Figure 8 - Demonstration Plan Statewide Map


Figure 9 - Demonstration Plan - Milwaukee Area


## b. Constitutional and Statutory Requirements

Table 5 shows the summary data for the Demonstration Plan (the full tables are in the annex to this report) and comparison data for the actual 2012 plan implemented in Act $43 .{ }^{24}$ The Demonstration Plan has a marginally larger population deviation, but is well below even the strictest standards applied to state legislative districts (a difference of $0.1 \%$ translates into 57 people). The population range in the Demonstration Plan is 57,191 to 57,686 , a difference of 495 people. Given the ideal Assembly district population of 57,444 , this is a deviation of $0.86 \%$. The Demonstration Plan is more compact on average than Act 43, and has fewer municipal splits (119 compared to 120 in Act 43). On all constitutional requirements, the Demonstration Plan is comparable to Act 43.

Table 5 - Plan Comparison to Act 43

|  | Demonstration <br> Plan | Act 43 |
| :---: | :---: | :---: |
| Population Deviation | $0.86 \%$ | $0.76 \%$ |
| Average Compactness (Reock) | 0.41 | 0.28 |
| Number of <br> Municipal Splits | County <br> City <br> Town <br> Village | 55 |

Act 43 created six majority-minority Black population districts (numbers 10-12 and 1618), ranging from $56.7 \%-67.6 \%$ Black population, and from $51.1 \%-61.8 \%$ Black voting age population. The Demonstration Plan retains six Majority Black Assembly districts, ranging from $60.0 \%$ to $63.4 \%$ Black population, and from $56.2 \%$ to $60.5 \%$ Black voting age population:

[^13]| Table 6 - Black Majority Districts in Demonstration Plan |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Assembly <br> District | Population | Voting Age <br> Population | Black <br> Population | Black <br> Percentage <br> of Population | Black <br> Voting Age <br> Population | BVAP\% |
| 10 | 57,195 | 41,528 | 36,593 | $64.0 \%$ | 25,125 | $60.5 \%$ |
| 11 | 57,455 | 40,510 | 34,822 | $60.6 \%$ | 22,762 | $56.2 \%$ |
| 12 | 57,420 | 38,774 | 34,923 | $60.8 \%$ | 21,829 | $56.3 \%$ |
| 16 | 57,282 | 42,469 | 36,321 | $63.4 \%$ | 23,920 | $56.3 \%$ |
| 17 | 57,437 | 39,639 | 34,450 | $60.0 \%$ | 22,275 | $56.2 \%$ |
| 18 | 57,241 | 40,840 | 35,316 | $61.7 \%$ | 24,054 | $58.9 \%$ |

In Baldus et al. v. Brennan et al., a federal Court created a majority Latino district in Milwaukee (the $8^{\text {th }}$ Assembly District). The Demonstration Plan retains the boundaries of this district thereby insuring compliance with Section 2 of the Voting Rights Act.

## C. Efficiency Gap Calculations

With the model described in Step one above and the block-level partisanship baseline it generates, I can analyze any existing or hypothetical district configuration and generate predicted vote totals and efficiency gap measures for the Demonstration Plan.

## 1. Analysis of Act 43

Any discussion of Act 43 must begin with the basic fact that in 2012 Republicans achieved a 60-39 majority in the Assembly in an election in which the Democratic Party achieved $53.5 \%$ of the statewide two-party presidential vote. The imbalance between the Republican Party's statewide vote margin at the top of the ticket (46.5\%) and its Assembly majority $(60.6 \%)$ turns the very notion of partisan symmetry on its head. That standard, according to King and Grofman $(2007,8)$ "requires that the number of seats one party would
receive if it garnered a particular percentage of the vote be identical to the number of seats the other party would receive if it had received the same percentage of the vote" $(2007,8)$. Here, it means that Democrats would have had to obtain 60 Assembly seats with $46.5 \%$ of the vote, an absurd proposition that requires a party's legislative seat share to go $u p$ as its share of the vote goes down.

This result was achieved via the classic gerrymandering strategies of packing and cracking. Figure 10, a histogram of Republican two party vote percentages in 2012, shows the pattern. Here, the bars to the right of $50 \%$ indicate a Republican victory. Twenty three Democratic candidates were uncontested, indicating a significant level of packing (the bar at the far left side of the figure); uncontested races occur largely when one party sees zero probability of winning because the majority party has such overwhelming majorities in the district. By contrast, only four Republicans were uncontested. Act 43 also successfully cracked Democratic majorities in other districts, creating Republican majorities that were either marginal (twelve in the $50-55 \%$ range) or relatively safe (thirty nine in the $55-65 \%$ range). The 2012 results are consistent with what was forecast in 2011, as shown by Figure 11, a histogram of Dr. Gaddie's baseline partisanship measure for Act 43 districts. This measure forecast fifty one Assembly districts with between $50 \%$ and $65 \%$ Republican vote share. This is the same number that actually occurred, fifty one.

Figure 12 shows the baseline partisanship district forecasts for Act 43, using the model outline in Step one, above. It is very similar to Dr. Gaddie's forecast and the actual results: it forecast fifty districts with between $50 \%$ and $65 \%$ Republican vote share.

Figure 10: Actual 2012 Republican Assembly Vote in Act 43 Districts


Figure 11: Republican Vote Forecast in Act 43 Districts - Gaddie Measure


Figure 12: Act 43 Baseline Partisan Measure


The treatment of the city of Sheboygan shows how this cracking was achieved.
Sheboygan is a city on the Lake Michigan shoreline with a population of 49,285. It is a strongly Democratic area, voting 58.7\%-41.3\% for Obama in 2012; my baseline partisanship estimate for the city is $58.2 \%$. The city is small enough to be contained in a single Assembly district in which it would constitute $86 \%$ of the ideal population, and it was entirely within the $26^{\text {th }}$ Assembly district in both the 1992 and 2001 redistricting rounds. The areas surrounding it the Village of Kohler and the Towns of Sheboygan and Wilson are all strongly Republican (with vote percentages for Romney of $62.8 \%, 56.3 \%$, and $59.4 \%$, respectively; together, these municipalities constitute an area that is $58.2 \%$ Republican, as measured by the presidential vote).

Keeping the city of Sheboygan together would have created a Democratic district, made up of the city itself ( $58.7 \%$ Democratic) with the remaining $14 \%$ of population drawn from one
of the Republican areas around it. The result would have been a District that was roughly $54 \%$ 56\% Democratic.

Act 43, however, split Sheboygan into separate Assembly districts, placing 32,640 residents of the city into the $26^{\text {th }}$ District, and 16,645 into the $27^{\text {th }}$. With the city split, these areas were combined into the Republican areas surrounding the city, producing two Republican districts: the $26^{\text {th }}(51.3 \%$ Republican in the 2012 Assembly race; baseline open seat partisanship measure of $53.3 \%$ ) and the $27^{\text {th }}$ ( $57.9 \%$ Republican in the 2012 Assembly race, baseline open seat partisanship measure of $52.3 \%$ ).

Figure 13, below, shows the split into Districts 26 and 27:


Figure 13-Act 43 Treatment of Sheboygan

## 2. Efficiency Gap Calculations for Act 43 and The Demonstration Plan

Recall that the efficiency gap is a measure of gerrymandering based on the difference in the number of "wasted votes." Votes cast for losing candidates are wasted, as are surplus votes for winning candidates above what is necessary to win. The gap is defined as the difference between the sum of wasted votes for the two parties, divided by the total number of votes cast in the election.

Comparing a hypothetical district plan (where vote totals are predicted) to an existing district plan (where vote totals are known) requires care, in large part because it can be difficult
to know with certainty what districts will have incumbents (or how incumbents might rearrange themselves after a redistricting cycle), and because not every district will be contested in an actual election (Stephanopoulos and McGhee 2015).

Handling uncontested races is a straightforward problem; the key is applying a consistent rule to all plans being compared. In the efficiency gap calculation for my plan, I measure underlying partisan strength in each district by estimating the number of votes that would be cast for each party in an open seat election each district, assuming that all races are contested. In the actual 2012 Assembly elections, only 72 of 99 seats were contested by both major parties, leaving 27 uncontested races. Uncontested races by themselves will not necessarily have a dramatic effect on efficiency gap calculations as long as the number of races is small, or if uncontested districts are evenly split between the parties (as a rule, one uncontested race with only a Democrat will cancel out one uncontested race with only a Republican, conditioned on the number of votes cast in each race). But a significant imbalance in uncontested races will have a material effect on the results. Of the 27 uncontested races in 2012, 23 were in Democratic districts and only 4 in Republican districts.

In the academic redistricting literature, uncontested seats are typically handled by imputing what the vote totals would have been if a race had been contested (Gelman and King 1990), or assigning each uncontested race a $75 \%-25 \%$ vote split in favor of the party whose candidate ran unopposed (Gelman and King 1994; Stephanopoulos and McGhee 2015). Because I have direct measures of partisanship and vote predictions, I am able to generate accurate estimates of what the vote totals would have been in Act 43's uncontested districts had both parties fielded candidates. In applying this method to the uncontested districts in the 2012 State Assembly elections, I create two directly equivalent sets of data: one for the Demonstration Plan,
with predicted values of open seat vote totals for all districts, and one for the districts created in Act 43, using open seat estimates for each district. Efficiency gap results for the two redistricting plans constructed this way can be compared directly.

Table 7 shows the full set of efficiency gap calculations for the Demonstration Plan, with incumbency effects removed. For each district I calculate an estimated Democratic and Republican vote total, and forecast a winner. The resulting columns show the number of "wasted votes," counting all votes cast for a losing candidates, and surplus votes for winning candidates (equal to $1 / 2$ of the margin of victory). Totals for each party are summed, and the efficiency gap calculated as the Net Wasted Votes (here, Democratic Wasted Votes - Republican Wasted Votes) divided by the total number of votes cast in the election.

The data in Table 7 (on page 48) show that the Demonstration Plan results in 741,984 wasted Democratic votes (column E), obtained by adding the number of lost Democratic votes cast for losing candidates ( 566,634 , column A) and the number of surplus Democratic votes cast for winners above what was necessary to win $(175,350$, column C). The same calculation for Republicans (using columns B and D) results in 689,570 wasted Republican votes. The difference between these two numbers, 781,984-689,570 $=62,414$ net wasted Democratic votes. Dividing 62,414 by the predicted total number of votes $2,843,108$, produces the baseline efficiency gap for my plan, .0220 , or $2.20 \%$.

Table 8 (on page 50 ) shows the same calculation for Act 43 districts, using estimated partisan vote totals with incumbent advantages removed. Act 43 resulted in a total of 332,552 net wasted Democratic votes. The efficiency gap of Act 43 is $11.69 \%$, more than five times larger than the Demonstration Plan.

Table 9 (on page 52) shows the efficiency gap calculation for the partisan baseline prediction used by Dr. Gaddie during the drawing of the Act 43 districts, applying his partisanship division to the total number of votes predicted from my model in each district. As described above in section $\operatorname{III}(\mathrm{B})(1)(\mathrm{h})$ above, this is the predicted baseline partisanship measure of Act 43. It produces a forecast Efficiency Gap for Act 43 of 12.36\%.

Table 10 summarizes these results:

|  | Table 10: Summary Statistics for Redistricting Plans |  |  |
| :---: | :---: | :---: | :---: |
|  | My Plan Baseline | Act 43 <br> Baseline | Act 43 - <br> Gaddie <br> Measure |
| party split (R-D) | 48-51 | 57-42 | 58-41 |
| Wasted Republican Votes | 679,570 | 544,893 | 535,057 |
| Wasted Democratic Votes | 741,984 | 877,445 | 886,403 |
| Gap | 62,414 | 332,552 | 351,346 |
| Total Democratic Votes | 1,454,117 | 1,454,717 | 1,394,018 |
| Total Republican Votes | 1,388,991 | 1,389,958 | 1,448,901 |
| Total Votes | 2,843,108 | 2,844,676 | 2,842,919 |
| Efficiency Gap (gap/total votes) | 2.20\% | 11.69\% | 12.36\% |

Three things are worth emphasizing. The first is that the predicted partisan effect of Act 43, represented by the Gaddie metric, produced an efficiency gap calculation (12.36\%) that was very close to the actual partisan effect of Act 43, as measured by the efficiency gap calculation for the actual 2012 partisan baseline (11.69\%). In brief, the architects of the Act 43 districts expected a partisan result that was almost identical to what actually occurred. The second is the large reduction in the efficiency gap that I am able to produce, which I have achieved without any departure from the core constitutional and statutory requirements of redistricting. The

Demonstration Plan is equivalent to Act 43 on all key criteria: population deviation, compactness, number of political subdivision splits, and compliance with the Voting Rights Act. At the same time, I have generated an efficiency gap score $82 \%$ smaller than the Act 43 gap. And third, I have reached this efficiency gap score with virtually identical numbers of Democratic and Republican voters as exist under Act 43. Given that my partisan estimates, once incumbency effects are removed, are entirely exogenous to any particular district configuration, these can be considered the same statewide set of voters. By placing the same voters as exist in Act 43 into a new set of districts designed to minimize the effects of gerrymandering while adhering to constitutional standards, I have generated a plan that is fair to both parties.

Figure 14 shows the distribution of baseline Republican vote predictions in the Demonstration Plan Assembly districts. The districts are far more balanced, with similar numbers of districts between $40 \%-50 \%$ (twenty seven) and between $50 \%-60 \%$ (twenty nine). There are also roughly equal numbers of districts above $65 \%$ (twelve) and below $35 \%$ (sixteen).

Figure 14: Predicted Vote - Demonstration Plan


Table 7-Efficiency Gap Calculation for Demonstration District Plan - No Incumbent Baseline

|  |  |  |  | A | B | C | D | E | F |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Assembly District | Predicted Democratic Votes | Predicted Republican Votes | Predicted <br> Winning <br> Party | Lost Democratic Votes | Lost Republican Votes | Surplus Democratic Votes | Surplus Republican Votes | Wasted Democratic Votes ( $\mathrm{A}+\mathrm{C}$ ) | Wasted Republican Votes (B+D) | Net Wasted Votes (E - F) |
| 1 | 16,259 | 16,414 | Republican | 16259 | 0 | 0 | 78 | 16259 | 78 | 16181 |
| 2 | 11,805 | 10,025 | Democratic | 0 | 10025 | 890 | 0 | 890 | 10025 | -9136 |
| 3 | 11,243 | 17,807 | Republican | 11243 | 0 | 0 | 3282 | 11243 | 3282 | 7961 |
| 4 | 10,881 | 12,790 | Republican | 10881 | 0 | 0 | 955 | 10881 | 955 | 9926 |
| 5 | 13,497 | 13,845 | Republican | 13497 | 0 | 0 | 174 | 13497 | 174 | 13323 |
| 6 | 11,045 | 17,627 | Republican | 11045 | 0 | 0 | 3291 | 11045 | 3291 | 7753 |
| 7 | 22,822 | 10,214 | Democratic | 0 | 10214 | 6304 | 0 | 6304 | 10214 | -3910 |
| 8 | 7,192 | 1,695 | Democratic | 0 | 1695 | 2749 | 0 | 2749 | 1695 | 1054 |
| 9 | 10,497 | 5,635 | Democratic | 0 | 5635 | 2431 | 0 | 2431 | 5635 | -3205 |
| 10 | 25,348 | 3,270 | Democratic | 0 | 3270 | 11039 | 0 | 11039 | 3270 | 7769 |
| 11 | 22,374 | 4,855 | Democratic | 0 | 4855 | 8759 | 0 | 8759 | 4855 | 3904 |
| 12 | 20,041 | 4,039 | Democratic | 0 | 4039 | 8001 | 0 | 8001 | 4039 | 3962 |
| 13 | 15,950 | 16,510 | Republican | 15950 | 0 | 0 | 280 | 15950 | 280 | 15670 |
| 14 | 13,575 | 13,799 | Republican | 13575 | 0 | 0 | 112 | 13575 | 112 | 13464 |
| 15 | 13,412 | 14,901 | Republican | 13412 | 0 | 0 | 745 | 13412 | 745 | 12667 |
| 16 | 21,234 | 2,856 | Democratic | 0 | 2856 | 9189 | 0 | 9189 | 2856 | 6333 |
| 17 | 21,769 | 3,569 | Democratic | 0 | 3569 | 9100 | 0 | 9100 | 3569 | 5531 |
| 18 | 23,817 | 4,954 | Democratic | 0 | 4954 | 9431 | 0 | 9431 | 4954 | 4477 |
| 19 | 15,160 | 10,904 | Democratic | 0 | 10904 | 2128 | 0 | 2128 | 10904 | -8776 |
| 20 | 14,118 | 12,901 | Democratic | 0 | 12901 | 609 | 0 | 609 | 12901 | -12292 |
| 21 | 12,257 | 16,911 | Republican | 12257 | 0 | 0 | 2327 | 12257 | 2327 | 9930 |
| 22 | 18,335 | 14,831 | Democratic | 0 | 14831 | 1752 | 0 | 1752 | 14831 | -13079 |
| 23 | 10,922 | 25,459 | Republican | 10922 | 0 | 0 | 7268 | 10922 | 7268 | 3654 |
| 24 | 8,667 | 25,868 | Republican | 8667 | 0 | 0 | 8601 | 8667 | 8601 | 66 |
| 25 | 12,179 | 18,248 | Republican | 12179 | 0 | 0 | 3034 | 12179 | 3034 | 9145 |
| 26 | 13,251 | 14,527 | Republican | 13251 | 0 | 0 | 638 | 13251 | 638 | 12613 |
| 27 | 14,935 | 11,755 | Democratic | 0 | 11755 | 1590 | 0 | 1590 | 11755 | -10165 |
| 28 | 12,617 | 15,591 | Republican | 12617 | 0 | 0 | 1487 | 12617 | 1487 | 11131 |
| 29 | 14,180 | 12,954 | Democratic | 0 | 12954 | 613 | 0 | 613 | 12954 | -12341 |
| 30 | 11,308 | 15,165 | Republican | 11308 | 0 | 0 | 1929 | 11308 | 1929 | 9379 |
| 31 | 11,304 | 16,117 | Republican | 11304 | 0 | 0 | 2406 | 11304 | 2406 | 8898 |
| 32 | 12,685 | 13,787 | Republican | 12685 | 0 | 0 | 551 | 12685 | 551 | 12135 |
| 33 | 14,609 | 10,151 | Democratic | 0 | 10151 | 2229 | 0 | 2229 | 10151 | -7922 |
| 34 | 13,139 | 15,690 | Republican | 13139 | 0 | 0 | 1275 | 13139 | 1275 | 11864 |
| 35 | 11,288 | 16,503 | Republican | 11288 | 0 | 0 | 2607 | 11288 | 2607 | 8681 |
| 36 | 11,516 | 14,997 | Republican | 11516 | 0 | 0 | 1741 | 11516 | 1741 | 9775 |
| 37 | 9,222 | 22,240 | Republican | 9222 | 0 | 0 | 6509 | 9222 | 6509 | 2713 |
| 38 | 9,710 | 25,021 | Republican | 9710 | 0 | 0 | 7655 | 9710 | 7655 | 2055 |
| 39 | 10,747 | 17,526 | Republican | 10747 | 0 | 0 | 3390 | 10747 | 3390 | 7357 |
| 40 | 15,061 | 13,947 | Democratic | 0 | 13947 | 557 | 0 | 557 | 13947 | -13391 |
| 41 | 16,784 | 13,120 | Democratic | 0 | 13120 | 1832 | 0 | 1832 | 13120 | -11288 |
| 42 | 13,254 | 12,282 | Democratic | 0 | 12282 | 486 | 0 | 486 | 12282 | -11796 |
| 43 | 12,658 | 13,606 | Republican | 12658 | 0 | 0 | 474 | 12658 | 474 | 12184 |
| 44 | 16,477 | 10,886 | Democratic | 0 | 10886 | 2795 | 0 | 2795 | 10886 | -8091 |
| 45 | 16,352 | 13,589 | Democratic | 0 | 13589 | 1382 | 0 | 1382 | 13589 | -12207 |
| 46 | 20,583 | 11,418 | Democratic | 0 | 11418 | 4582 | 0 | 4582 | 11418 | -6835 |
| 47 | 20,208 | 9,888 | Democratic | 0 | 9888 | 5160 | 0 | 5160 | 9888 | -4728 |


| 48 | 24,457 | 8,840 | Democratic | 0 | 8840 | 7808 | 0 | 7808 | 8840 | -1032 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 49 | 13,625 | 13,477 | Democratic | 0 | 13477 | 74 | 0 | 74 | 13477 | -13403 |
| 50 | 12,289 | 13,709 | Republican | 12289 | 0 | 0 | 710 | 12289 | 710 | 11579 |
| 51 | 14,760 | 13,323 | Democratic | 0 | 13323 | 718 | 0 | 718 | 13323 | -12605 |
| 52 | 12,376 | 19,416 | Republican | 12376 | 0 | 0 | 3520 | 12376 | 3520 | 8857 |
| 53 | 12,388 | 13,362 | Republican | 12388 | 0 | 0 | 487 | 12388 | 487 | 11902 |
| 54 | 14,032 | 12,240 | Democratic | 0 | 12240 | 896 | 0 | 896 | 12240 | -11344 |
| 55 | 13,565 | 15,300 | Republican | 13565 | 0 | 0 | 868 | 13565 | 868 | 12697 |
| 56 | 12,553 | 14,518 | Republican | 12553 | 0 | 0 | 983 | 12553 | 983 | 11570 |
| 57 | 14,897 | 13,016 | Democratic | 0 | 13016 | 941 | 0 | 941 | 13016 | -12075 |
| 58 | 9,325 | 21,180 | Republican | 9325 | 0 | 0 | 5927 | 9325 | 5927 | 3398 |
| 59 | 11,565 | 21,984 | Republican | 11565 | 0 | 0 | 5209 | 11565 | 5209 | 6356 |
| 60 | 8,756 | 22,415 | Republican | 8756 | 0 | 0 | 6830 | 8756 | 6830 | 1926 |
| 61 | 12,933 | 16,576 | Republican | 12933 | 0 | 0 | 1822 | 12933 | 1822 | 11112 |
| 62 | 15,181 | 9,999 | Democratic | 0 | 9999 | 2591 | 0 | 2591 | 9999 | -7408 |
| 63 | 15,640 | 9,902 | Democratic | 0 | 9902 | 2869 | 0 | 2869 | 9902 | -7033 |
| 64 | 15,089 | 13,470 | Democratic | 0 | 13470 | 810 | 0 | 810 | 13470 | -12660 |
| 65 | 12,721 | 19,816 | Republican | 12721 | 0 | 0 | 3547 | 12721 | 3547 | 9173 |
| 66 | 16,286 | 6,362 | Democratic | 0 | 6362 | 4962 | 0 | 4962 | 6362 | -1401 |
| 67 | 15,321 | 14,226 | Democratic | 0 | 14226 | 547 | 0 | 547 | 14226 | -13678 |
| 68 | 11,958 | 12,124 | Republican | 11958 | 0 | 0 | 83 | 11958 | 83 | 11875 |
| 69 | 17,902 | 12,022 | Democratic | 0 | 12022 | 2940 | 0 | 2940 | 12022 | -9083 |
| 70 | 18,661 | 12,266 | Democratic | 0 | 12266 | 3197 | 0 | 3197 | 12266 | -9069 |
| 71 | 15,081 | 13,884 | Democratic | 0 | 13884 | 599 | 0 | 599 | 13884 | -13285 |
| 72 | 11,180 | 16,542 | Republican | 11180 | 0 | 0 | 2681 | 11180 | 2681 | 8500 |
| 73 | 17,137 | 10,785 | Democratic | 0 | 10785 | 3176 | 0 | 3176 | 10785 | -7609 |
| 74 | 17,712 | 14,219 | Democratic | 0 | 14219 | 1747 | 0 | 1747 | 14219 | -12472 |
| 75 | 13,902 | 17,700 | Republican | 13902 | 0 | 0 | 1899 | 13902 | 1899 | 12002 |
| 76 | 30,929 | 6,811 | Democratic | 0 | 6811 | 12059 | 0 | 12059 | 6811 | 5248 |
| 77 | 26,708 | 6,059 | Democratic | 0 | 6059 | 10325 | 0 | 10325 | 6059 | 4266 |
| 78 | 24,413 | 9,847 | Democratic | 0 | 9847 | 7283 | 0 | 7283 | 9847 | -2564 |
| 79 | 20,439 | 13,294 | Democratic | 0 | 13294 | 3572 | 0 | 3572 | 13294 | -9722 |
| 80 | 20,179 | 11,644 | Democratic | 0 | 11644 | 4267 | 0 | 4267 | 11644 | -7377 |
| 81 | 13,703 | 12,741 | Democratic | 0 | 12741 | 481 | 0 | 481 | 12741 | -12260 |
| 82 | 9,871 | 21,201 | Republican | 9871 | 0 | 0 | 5665 | 9871 | 5665 | 4206 |
| 83 | 9,241 | 23,075 | Republican | 9241 | 0 | 0 | 6917 | 9241 | 6917 | 2324 |
| 84 | 11,990 | 22,700 | Republican | 11990 | 0 | 0 | 5355 | 11990 | 5355 | 6634 |
| 85 | 10,028 | 13,190 | Republican | 10028 | 0 | 0 | 1581 | 10028 | 1581 | 8448 |
| 86 | 13,853 | 13,494 | Democratic | 0 | 13494 | 180 | 0 | 180 | 13494 | -13314 |
| 87 | 11,358 | 17,003 | Republican | 11358 | 0 | 0 | 2823 | 11358 | 2823 | 8535 |
| 88 | 14,209 | 11,142 | Democratic | 0 | 11142 | 1533 | 0 | 1533 | 11142 | -9609 |
| 89 | 13,374 | 15,771 | Republican | 13374 | 0 | 0 | 1199 | 13374 | 1199 | 12175 |
| 90 | 11,349 | 17,468 | Republican | 11349 | 0 | 0 | 3059 | 11349 | 3059 | 8290 |
| 91 | 14,807 | 13,845 | Democratic | 0 | 13845 | 481 | 0 | 481 | 13845 | -13364 |
| 92 | 14,907 | 14,594 | Democratic | 0 | 14594 | 157 | 0 | 157 | 14594 | -14437 |
| 93 | 12,441 | 18,057 | Republican | 12441 | 0 | 0 | 2808 | 12441 | 2808 | 9633 |
| 94 | 16,171 | 11,759 | Democratic | 0 | 11759 | 2206 | 0 | 2206 | 11759 | -9553 |
| 95 | 19,769 | 9,949 | Democratic | 0 | 9949 | 4910 | 0 | 4910 | 9949 | -5040 |
| 96 | 14,665 | 13,836 | Democratic | 0 | 13836 | 415 | 0 | 415 | 13836 | -13421 |
| 97 | 11,492 | 24,222 | Republican | 11492 | 0 | 0 | 6365 | 11492 | 6365 | 5128 |
| 98 | 9,864 | 24,773 | Republican | 9864 | 0 | 0 | 7454 | 9864 | 7454 | 2410 |
| 99 | 10,783 | 19,160 | Republican | 10783 | 0 | 0 | 4188 | 10783 | 4188 | 6594 |
| TOTALS | 1,454,117 | 1,388,991 |  | 566,634 | 536,783 | 175,350 | 142,787 | 741,984 | 679,570 | 62,414 |

Table 8 - Efficiency Gap Calculation for Act 43 - No Incumbent Baseline

|  |  |  |  | A | B | C | D | E | F |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Assembly District | Predicted <br> Democratic <br> Votes | Predicted Republican Votes | Predicted Winning Party | Lost <br> Democratic Votes | Lost Republican Votes | Surplus Democra tic Votes | Surplus Republic an Votes | Wasted Democratic Votes $(A+C)$ | Wasted Republican Votes (B + D) | Net <br> Wasted <br> Votes <br> (E-F) <br> ( |
| 1 | 16,235 | 16,628 | Republican | 16235 | 0 | 0 | 197 | 16235 | 197 | 16038 |
| 2 | 12,398 | 16,357 | Republican | 12398 | 0 | 0 | 1980 | 12398 | 1980 | 10419 |
| 3 | 12,623 | 16,636 | Republican | 12623 | 0 | 0 | 2006 | 12623 | 2006 | 10617 |
| 4 | 13,926 | 15,576 | Republican | 13926 | 0 | 0 | 825 | 13926 | 825 | 13101 |
| 5 | 12,710 | 16,017 | Republican | 12710 | 0 | 0 | 1654 | 12710 | 1654 | 11056 |
| 6 | 10,929 | 14,938 | Republican | 10929 | 0 | 0 | 2005 | 10929 | 2005 | 8924 |
| 7 | 13,793 | 11,778 | Democratic | 0 | 11778 | 1007 | 0 | 1007 | 11778 | -10771 |
| 8 | 7,342 | 1,738 | Democratic | 0 | 1738 | 2802 | 0 | 2802 | 1738 | 1064 |
| 9 | 10,023 | 4,533 | Democratic | 0 | 4533 | 2745 | 0 | 2745 | 4533 | -1787 |
| 10 | 25,306 | 2,897 | Democratic | 0 | 2897 | 11205 | 0 | 11205 | 2897 | 8308 |
| 11 | 21,698 | 3,368 | Democratic | 0 | 3368 | 9165 | 0 | 9165 | 3368 | 5797 |
| 12 | 19,700 | 5,222 | Democratic | 0 | 5222 | 7239 | 0 | 7239 | 5222 | 2018 |
| 13 | 13,345 | 20,358 | Republican | 13345 | 0 | 0 | 3506 | 13345 | 3506 | 9839 |
| 14 | 14,499 | 21,025 | Republican | 14499 | 0 | 0 | 3263 | 14499 | 3263 | 11235 |
| 15 | 13,006 | 17,310 | Republican | 13006 | 0 | 0 | 2152 | 13006 | 2152 | 10853 |
| 16 | 22,293 | 2,342 | Democratic | 0 | 2342 | 9975 | 0 | 9975 | 2342 | 7633 |
| 17 | 24,088 | 4,047 | Democratic | 0 | 4047 | 10020 | 0 | 10020 | 4047 | 5973 |
| 18 | 22,204 | 2,692 | Democratic | 0 | 2692 | 9756 | 0 | 9756 | 2692 | 7064 |
| 19 | 22,759 | 10,364 | Democratic | 0 | 10364 | 6198 | 0 | 6198 | 10364 | -4166 |
| 20 | 16,066 | 12,856 | Democratic | 0 | 12856 | 1605 | 0 | 1605 | 12856 | -11252 |
| 21 | 12,566 | 15,324 | Republican | 12566 | 0 | 0 | 1379 | 12566 | 1379 | 11187 |
| 22 | 11,290 | 22,958 | Republican | 11290 | 0 | 0 | 5834 | 11290 | 5834 | 5456 |
| 23 | 14,260 | 21,633 | Republican | 14260 | 0 | 0 | 3687 | 14260 | 3687 | 10573 |
| 24 | 13,885 | 20,335 | Republican | 13885 | 0 | 0 | 3225 | 13885 | 3225 | 10659 |
| 25 | 12,032 | 15,933 | Republican | 12032 | 0 | 0 | 1950 | 12032 | 1950 | 10082 |
| 26 | 13,639 | 15,559 | Republican | 13639 | 0 | 0 | 960 | 13639 | 960 | 12679 |
| 27 | 14,709 | 16,360 | Republican | 14709 | 0 | 0 | 826 | 14709 | 826 | 13883 |
| 28 | 12,719 | 15,302 | Republican | 12719 | 0 | 0 | 1291 | 12719 | 1291 | 11428 |
| 29 | 12,909 | 14,662 | Republican | 12909 | 0 | 0 | 876 | 12909 | 876 | 12033 |
| 30 | 14,019 | 16,951 | Republican | 14019 | 0 | 0 | 1466 | 14019 | 1466 | 12553 |
| 31 | 13,273 | 15,615 | Republican | 13273 | 0 | 0 | 1171 | 13273 | 1171 | 12102 |
| 32 | 11,255 | 15,359 | Republican | 11255 | 0 | 0 | 2052 | 11255 | 2052 | 9203 |
| 33 | 11,226 | 18,298 | Republican | 11226 | 0 | 0 | 3536 | 11226 | 3536 | 7690 |
| 34 | 12,445 | 19,355 | Republican | 12445 | 0 | 0 | 3455 | 12445 | 3455 | 8991 |
| 35 | 12,270 | 15,525 | Republican | 12270 | 0 | 0 | 1628 | 12270 | 1628 | 10643 |
| 36 | 11,403 | 15,672 | Republican | 11403 | 0 | 0 | 2134 | 11403 | 2134 | 9269 |
| 37 | 12,707 | 16,202 | Republican | 12707 | 0 | 0 | 1747 | 12707 | 1747 | 10960 |
| 38 | 12,668 | 19,129 | Republican | 12668 | 0 | 0 | 3231 | 12668 | 3231 | 9437 |
| 39 | 11,491 | 17,211 | Republican | 11491 | 0 | 0 | 2860 | 11491 | 2860 | 8630 |
| 40 | 11,485 | 13,597 | Republican | 11485 | 0 | 0 | 1056 | 11485 | 1056 | 10429 |
| 41 | 11,719 | 14,492 | Republican | 11719 | 0 | 0 | 1387 | 11719 | 1387 | 10332 |
| 42 | 13,705 | 15,462 | Republican | 13705 | 0 | 0 | 879 | 13705 | 879 | 12826 |
| 43 | 17,380 | 13,075 | Democratic | 0 | 13075 | 2153 | 0 | 2153 | 13075 | -10923 |
| 44 | 16,680 | 10,304 | Democratic | 0 | 10304 | 3188 | 0 | 3188 | 10304 | -7116 |
| 45 | 15,153 | 9,691 | Democratic | 0 | 9691 | 2731 | 0 | 2731 | 9691 | -6959 |
| 46 | 19,173 | 11,534 | Democratic | 0 | 11534 | 3819 | 0 | 3819 | 11534 | -7714 |
| 47 | 21,609 | 9,340 | Democratic | 0 | 9340 | 6135 | 0 | 6135 | 9340 | -3205 |
| 48 | 24,517 | 7,635 | Democratic | 0 | 7635 | 8441 | 0 | 8441 | 7635 | 806 |
| 49 | 12,307 | 13,621 | Republican | 12307 | 0 | 0 | 657 | 12307 | 657 | 11650 |


| 50 | 12,467 | 12,326 | Democratic | 0 | 12326 | 71 | 0 | 71 | 12326 | -12256 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 51 | 14,173 | 13,048 | Democratic | 0 | 13048 | 563 | 0 | 563 | 13048 | -12485 |
| 52 | 11,294 | 15,656 | Republican | 11294 | 0 | 0 | 2181 | 11294 | 2181 | 9113 |
| 53 | 9,875 | 16,753 | Republican | 9875 | 0 | 0 | 3439 | 9875 | 3439 | 6437 |
| 54 | 15,180 | 12,882 | Democratic | 0 | 12882 | 1149 | 0 | 1149 | 12882 | -11733 |
| 55 | 12,634 | 16,971 | Republican | 12634 | 0 | 0 | 2169 | 12634 | 2169 | 10465 |
| 56 | 12,564 | 18,576 | Republican | 12564 | 0 | 0 | 3006 | 12564 | 3006 | 9559 |
| 57 | 14,387 | 11,676 | Democratic | 0 | 11676 | 1355 | 0 | 1355 | 11676 | -10321 |
| 58 | 8,843 | 22,417 | Republican | 8843 | 0 | 0 | 6787 | 8843 | 6787 | 2055 |
| 59 | 8,784 | 21,725 | Republican | 8784 | 0 | 0 | 6471 | 8784 | 6471 | 2313 |
| 60 | 9,848 | 23,989 | Republican | 9848 | 0 | 0 | 7071 | 9848 | 7071 | 2778 |
| 61 | 13,145 | 16,481 | Republican | 13145 | 0 | 0 | 1668 | 13145 | 1668 | 11477 |
| 62 | 14,828 | 17,309 | Republican | 14828 | 0 | 0 | 1240 | 14828 | 1240 | 13588 |
| 63 | 13,233 | 16,830 | Republican | 13233 | 0 | 0 | 1799 | 13233 | 1799 | 11434 |
| 64 | 15,702 | 11,307 | Democratic | 0 | 11307 | 2198 | 0 | 2198 | 11307 | -9109 |
| 65 | 15,105 | 7,929 | Democratic | 0 | 7929 | 3588 | 0 | 3588 | 7929 | -4341 |
| 66 | 16,162 | 5,472 | Democratic | 0 | 5472 | 5345 | 0 | 5345 | 5472 | -127 |
| 67 | 13,769 | 14,674 | Republican | 13769 | 0 | 0 | 453 | 13769 | 453 | 13316 |
| 68 | 13,663 | 13,005 | Democratic | 0 | 13005 | 329 | 0 | 329 | 13005 | -12676 |
| 69 | 11,083 | 14,347 | Republican | 11083 | 0 | 0 | 1632 | 11083 | 1632 | 9451 |
| 70 | 12,211 | 14,387 | Republican | 12211 | 0 | 0 | 1088 | 12211 | 1088 | 11123 |
| 71 | 17,614 | 11,383 | Democratic | 0 | 11383 | 3115 | 0 | 3115 | 11383 | -8267 |
| 72 | 14,294 | 13,895 | Democratic | 0 | 13895 | 199 | 0 | 199 | 13895 | -13696 |
| 73 | 17,353 | 10,784 | Democratic | 0 | 10784 | 3284 | 0 | 3284 | 10784 | -7500 |
| 74 | 17,095 | 13,772 | Democratic | 0 | 13772 | 1662 | 0 | 1662 | 13772 | -12110 |
| 75 | 15,000 | 13,418 | Democratic | 0 | 13418 | 791 | 0 | 791 | 13418 | -12627 |
| 76 | 30,939 | 6,805 | Democratic | 0 | 6805 | 12067 | 0 | 12067 | 6805 | 5262 |
| 77 | 26,925 | 6,041 | Democratic | 0 | 6041 | 10442 | 0 | 10442 | 6041 | 4402 |
| 78 | 24,163 | 9,857 | Democratic | 0 | 9857 | 7153 | 0 | 7153 | 9857 | -2704 |
| 79 | 20,753 | 13,975 | Democratic | 0 | 13975 | 3389 | 0 | 3389 | 13975 | -10586 |
| 80 | 20,369 | 12,604 | Democratic | 0 | 12604 | 3882 | 0 | 3882 | 12604 | -8722 |
| 81 | 16,310 | 12,356 | Democratic | 0 | 12356 | 1977 | 0 | 1977 | 12356 | -10379 |
| 82 | 12,168 | 18,085 | Republican | 12168 | 0 | 0 | 2959 | 12168 | 2959 | 9210 |
| 83 | 10,186 | 23,755 | Republican | 10186 | 0 | 0 | 6784 | 10186 | 6784 | 3401 |
| 84 | 12,503 | 18,765 | Republican | 12503 | 0 | 0 | 3131 | 12503 | 3131 | 9373 |
| 85 | 13,613 | 12,925 | Democratic | 0 | 12925 | 344 | 0 | 344 | 12925 | -12581 |
| 86 | 13,425 | 17,152 | Republican | 13425 | 0 | 0 | 1863 | 13425 | 1863 | 11561 |
| 87 | 11,780 | 15,118 | Republican | 11780 | 0 | 0 | 1669 | 11780 | 1669 | 10111 |
| 88 | 13,141 | 14,380 | Republican | 13141 | 0 | 0 | 620 | 13141 | 620 | 12521 |
| 89 | 11,610 | 15,516 | Republican | 11610 | 0 | 0 | 1953 | 11610 | 1953 | 9658 |
| 90 | 12,080 | 7,309 | Democratic | 0 | 7309 | 2385 | 0 | 2385 | 7309 | -4924 |
| 91 | 17,942 | 11,769 | Democratic | 0 | 11769 | 3086 | 0 | 3086 | 11769 | -8683 |
| 92 | 14,285 | 11,441 | Democratic | 0 | 11441 | 1422 | 0 | 1422 | 11441 | -10019 |
| 93 | 15,268 | 15,393 | Republican | 15268 | 0 | 0 | 62 | 15268 | 62 | 15206 |
| 94 | 17,408 | 12,954 | Democratic | 0 | 12954 | 2227 | 0 | 2227 | 12954 | -10727 |
| 95 | 19,804 | 9,627 | Democratic | 0 | 9627 | 5088 | 0 | 5088 | 9627 | -4539 |
| 96 | 10,950 | 14,873 | Republican | 10950 | 0 | 0 | 1962 | 10950 | 1962 | 8989 |
| 97 | 10,826 | 18,042 | Republican | 10826 | 0 | 0 | 3608 | 10826 | 3608 | 7219 |
| 98 | 10,182 | 21,855 | Republican | 10182 | 0 | 0 | 5837 | 10182 | 5837 | 4346 |
| 99 | 8,346 | 25,535 | Republican | 8346 | 0 | 0 | 8594 | 8346 | 8594 | -248 |
| TOTALS | 1,454,717 | 1,389,958 |  | 702,148 | 401,975 | 175,297 | 142,918 | 877,445 | 544,893 | 332,552 |

Table 9 - Efficiency Gap Calculation for
Act 432011 Gaddie Metric - No Incumbent Baseline

|  |  |  |  | A | B | C | D | E | F |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Assembly District | Predicted Democratic Votes | Predicted Republican Votes | Predicted Winning Party | Lost Democratic Votes | Lost Republican Votes | Surplus Democratic Votes | Surplus Republican Votes | Wasted Democratic Votes (A + C) | Wasted Republican Votes (B+D) | Net Wasted Votes (E - F) |
| 1 | 15,857 | 16,651 | Republican | 15857 | 0 | 0 | 397 | 15857 | 397 | 15461 |
| 2 | 12,983 | 15,766 | Republican | 12983 | 0 | 0 | 1391 | 12983 | 1391 | 11591 |
| 3 | 12,976 | 16,236 | Republican | 12976 | 0 | 0 | 1630 | 12976 | 1630 | 11346 |
| 4 | 13,742 | 15,791 | Republican | 13742 | 0 | 0 | 1025 | 13742 | 1025 | 12717 |
| 5 | 13,134 | 15,593 | Republican | 13134 | 0 | 0 | 1230 | 13134 | 1230 | 11904 |
| 6 | 10,779 | 15,088 | Republican | 10779 | 0 | 0 | 2155 | 10779 | 2155 | 8624 |
| 7 | 13,967 | 11,604 | Democratic | 0 | 11604 | 1181 | 0 | 1181 | 11604 | -10423 |
| 8 | 6,178 | 2,709 | Democratic | 0 | 2709 | 1735 | 0 | 1735 | 2709 | -974 |
| 9 | 10,173 | 4,184 | Democratic | 0 | 4184 | 2995 | 0 | 2995 | 4184 | -1189 |
| 10 | 24,623 | 3,547 | Democratic | 0 | 3547 | 10538 | 0 | 10538 | 3547 | 6992 |
| 11 | 20,235 | 4,927 | Democratic | 0 | 4927 | 7654 | 0 | 7654 | 4927 | 2728 |
| 12 | 18,066 | 6,856 | Democratic | 0 | 6856 | 5605 | 0 | 5605 | 6856 | -1251 |
| 13 | 13,929 | 19,774 | Republican | 13929 | 0 | 0 | 2922 | 13929 | 2922 | 11007 |
| 14 | 14,693 | 20,831 | Republican | 14693 | 0 | 0 | 3069 | 14693 | 3069 | 11624 |
| 15 | 13,497 | 16,819 | Republican | 13497 | 0 | 0 | 1661 | 13497 | 1661 | 11835 |
| 16 | 22,223 | 2,618 | Democratic | 0 | 2618 | 9803 | 0 | 9803 | 2618 | 7184 |
| 17 | 22,553 | 5,582 | Democratic | 0 | 5582 | 8486 | 0 | 8486 | 5582 | 2904 |
| 18 | 21,176 | 3,719 | Democratic | 0 | 3719 | 8728 | 0 | 8728 | 3719 | 5009 |
| 19 | 23,838 | 9,284 | Democratic | 0 | 9284 | 7277 | 0 | 7277 | 9284 | -2007 |
| 20 | 16,451 | 12,471 | Democratic | 0 | 12471 | 1990 | 0 | 1990 | 12471 | -10482 |
| 21 | 13,125 | 14,765 | Republican | 13125 | 0 | 0 | 820 | 13125 | 820 | 12305 |
| 22 | 11,364 | 22,885 | Republican | 11364 | 0 | 0 | 5761 | 11364 | 5761 | 5603 |
| 23 | 15,182 | 20,658 | Republican | 15182 | 0 | 0 | 2738 | 15182 | 2738 | 12444 |
| 24 | 14,205 | 20,015 | Republican | 14205 | 0 | 0 | 2905 | 14205 | 2905 | 11299 |
| 25 | 13,065 | 14,887 | Republican | 13065 | 0 | 0 | 911 | 13065 | 911 | 12154 |
| 26 | 12,853 | 16,338 | Republican | 12853 | 0 | 0 | 1743 | 12853 | 1743 | 11110 |
| 27 | 13,611 | 17,458 | Republican | 13611 | 0 | 0 | 1923 | 13611 | 1923 | 11688 |
| 28 | 12,609 | 15,412 | Republican | 12609 | 0 | 0 | 1401 | 12609 | 1401 | 11208 |
| 29 | 13,519 | 14,054 | Republican | 13519 | 0 | 0 | 267 | 13519 | 267 | 13251 |
| 30 | 14,267 | 16,601 | Republican | 14267 | 0 | 0 | 1167 | 14267 | 1167 | 13101 |
| 31 | 12,616 | 16,273 | Republican | 12616 | 0 | 0 | 1829 | 12616 | 1829 | 10787 |
| 32 | 10,038 | 16,566 | Republican | 10038 | 0 | 0 | 3264 | 10038 | 3264 | 6773 |
| 33 | 11,274 | 18,247 | Republican | 11274 | 0 | 0 | 3487 | 11274 | 3487 | 7788 |
| 34 | 14,239 | 17,558 | Republican | 14239 | 0 | 0 | 1660 | 14239 | 1660 | 12579 |
| 35 | 13,067 | 14,729 | Republican | 13067 | 0 | 0 | 831 | 13067 | 831 | 12236 |
| 36 | 12,227 | 14,848 | Republican | 12227 | 0 | 0 | 1310 | 12227 | 1310 | 10917 |
| 37 | 12,110 | 16,799 | Republican | 12110 | 0 | 0 | 2345 | 12110 | 2345 | 9766 |
| 38 | 12,574 | 19,218 | Republican | 12574 | 0 | 0 | 3322 | 12574 | 3322 | 9251 |
| 39 | 10,899 | 17,782 | Republican | 10899 | 0 | 0 | 3442 | 10899 | 3442 | 7457 |
| 40 | 10,514 | 14,561 | Republican | 10514 | 0 | 0 | 2024 | 10514 | 2024 | 8490 |
| 41 | 11,761 | 14,467 | Republican | 11761 | 0 | 0 | 1353 | 11761 | 1353 | 10407 |
| 42 | 13,152 | 16,036 | Republican | 13152 | 0 | 0 | 1442 | 13152 | 1442 | 11710 |
| 43 | 17,339 | 13,113 | Democratic | 0 | 13113 | 2113 | 0 | 2113 | 13113 | -10999 |
| 44 | 16,941 | 10,043 | Democratic | 0 | 10043 | 3449 | 0 | 3449 | 10043 | -6595 |
| 45 | 14,886 | 9,957 | Democratic | 0 | 9957 | 2464 | 0 | 2464 | 9957 | -7493 |
| 46 | 17,681 | 13,010 | Democratic | 0 | 13010 | 2336 | 0 | 2336 | 13010 | -10674 |


| 47 | 20,628 | 10,322 | Democratic | 0 | 10322 | 5153 | 0 | 5153 | 10322 | -5169 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 48 | 23,290 | 8,861 | Democratic | 0 | 8861 | 7215 | 0 | 7215 | 8861 | -1646 |
| 49 | 13,071 | 12,859 | Democratic | 0 | 12859 | 106 | 0 | 106 | 12859 | -12752 |
| 50 | 11,887 | 12,908 | Republican | 11887 | 0 | 0 | 511 | 11887 | 511 | 11376 |
| 51 | 14,637 | 12,584 | Democratic | 0 | 12584 | 1026 | 0 | 1026 | 12584 | -11558 |
| 52 | 11,034 | 15,918 | Republican | 11034 | 0 | 0 | 2442 | 11034 | 2442 | 8592 |
| 53 | 9,930 | 16,099 | Republican | 9930 | 0 | 0 | 3084 | 9930 | 3084 | 6846 |
| 54 | 15,372 | 12,690 | Democratic | 0 | 12690 | 1341 | 0 | 1341 | 12690 | -11348 |
| 55 | 13,302 | 16,297 | Republican | 13302 | 0 | 0 | 1498 | 13302 | 1498 | 11804 |
| 56 | 12,809 | 18,326 | Republican | 12809 | 0 | 0 | 2759 | 12809 | 2759 | 10050 |
| 57 | 14,436 | 11,575 | Democratic | 0 | 11575 | 1431 | 0 | 1431 | 11575 | -10145 |
| 58 | 9,211 | 22,056 | Republican | 9211 | 0 | 0 | 6422 | 9211 | 6422 | 2789 |
| 59 | 9,669 | 20,843 | Republican | 9669 | 0 | 0 | 5587 | 9669 | 5587 | 4083 |
| 60 | 10,307 | 23,508 | Republican | 10307 | 0 | 0 | 6601 | 10307 | 6601 | 3706 |
| 61 | 12,661 | 16,935 | Republican | 12661 | 0 | 0 | 2137 | 12661 | 2137 | 10524 |
| 62 | 13,959 | 18,175 | Republican | 13959 | 0 | 0 | 2108 | 13959 | 2108 | 11851 |
| 63 | 11,973 | 17,692 | Republican | 11973 | 0 | 0 | 2860 | 11973 | 2860 | 9113 |
| 64 | 15,452 | 11,524 | Democratic | 0 | 11524 | 1964 | 0 | 1964 | 11524 | -9560 |
| 65 | 14,760 | 8,274 | Democratic | 0 | 8274 | 3243 | 0 | 3243 | 8274 | -5031 |
| 66 | 14,776 | 6,861 | Democratic | 0 | 6861 | 3957 | 0 | 3957 | 6861 | -2904 |
| 67 | 13,748 | 14,698 | Republican | 13748 | 0 | 0 | 475 | 13748 | 475 | 13273 |
| 68 | 13,508 | 13,177 | Democratic | 0 | 13177 | 165 | 0 | 165 | 13177 | -13011 |
| 69 | 11,657 | 13,773 | Republican | 11657 | 0 | 0 | 1058 | 11657 | 1058 | 10599 |
| 70 | 13,105 | 13,493 | Republican | 13105 | 0 | 0 | 194 | 13105 | 194 | 12911 |
| 71 | 17,189 | 11,807 | Democratic | 0 | 11807 | 2691 | 0 | 2691 | 11807 | -9116 |
| 72 | 13,674 | 14,514 | Republican | 13674 | 0 | 0 | 420 | 13674 | 420 | 13254 |
| 73 | 16,837 | 11,300 | Democratic | 0 | 11300 | 2769 | 0 | 2769 | 11300 | -8531 |
| 74 | 17,628 | 13,239 | Democratic | 0 | 13239 | 2195 | 0 | 2195 | 13239 | -11044 |
| 75 | 13,590 | 14,829 | Republican | 13590 | 0 | 0 | 620 | 13590 | 620 | 12970 |
| 76 | 32,275 | 5,469 | Democratic | 0 | 5469 | 13403 | 0 | 13403 | 5469 | 7934 |
| 77 | 26,627 | 6,339 | Democratic | 0 | 6339 | 10144 | 0 | 10144 | 6339 | 3804 |
| 78 | 23,528 | 10,492 | Democratic | 0 | 10492 | 6518 | 0 | 6518 | 10492 | -3974 |
| 79 | 20,211 | 14,516 | Democratic | 0 | 14516 | 2848 | 0 | 2848 | 14516 | -11668 |
| 80 | 20,251 | 12,704 | Democratic | 0 | 12704 | 3773 | 0 | 3773 | 12704 | -8931 |
| 81 | 15,887 | 12,770 | Democratic | 0 | 12770 | 1559 | 0 | 1559 | 12770 | -11211 |
| 82 | 12,985 | 17,269 | Republican | 12985 | 0 | 0 | 2142 | 12985 | 2142 | 10843 |
| 83 | 10,756 | 23,185 | Republican | 10756 | 0 | 0 | 6215 | 10756 | 6215 | 4541 |
| 84 | 13,414 | 17,854 | Republican | 13414 | 0 | 0 | 2220 | 13414 | 2220 | 11194 |
| 85 | 13,703 | 12,843 | Democratic | 0 | 12843 | 430 | 0 | 430 | 12843 | -12413 |
| 86 | 15,780 | 14,789 | Democratic | 0 | 14789 | 495 | 0 | 495 | 14789 | -14294 |
| 87 | 12,413 | 14,420 | Republican | 12413 | 0 | 0 | 1004 | 12413 | 1004 | 11409 |
| 88 | 12,882 | 14,638 | Republican | 12882 | 0 | 0 | 878 | 12882 | 878 | 12004 |
| 89 | 12,009 | 15,118 | Republican | 12009 | 0 | 0 | 1554 | 12009 | 1554 | 10455 |
| 90 | 11,556 | 7,833 | Democratic | 0 | 7833 | 1861 | 0 | 1861 | 7833 | -5972 |
| 91 | 18,044 | 11,816 | Democratic | 0 | 11816 | 3114 | 0 | 3114 | 11816 | -8701 |
| 92 | 14,313 | 11,383 | Democratic | 0 | 11383 | 1465 | 0 | 1465 | 11383 | -9919 |
| 93 | 15,014 | 15,690 | Republican | 15014 | 0 | 0 | 338 | 15014 | 338 | 14676 |
| 94 | 14,601 | 15,761 | Republican | 14601 | 0 | 0 | 580 | 14601 | 580 | 14022 |
| 95 | 18,730 | 10,701 | Democratic | 0 | 10701 | 4014 | 0 | 4014 | 10701 | -6687 |
| 96 | 13,841 | 11,982 | Democratic | 0 | 11982 | 930 | 0 | 930 | 11982 | -11052 |
| 97 | 10,706 | 18,158 | Republican | 10706 | 0 | 0 | 3726 | 10706 | 3726 | 6979 |
| 98 | 10,566 | 21,472 | Republican | 10566 | 0 | 0 | 5453 | 10566 | 5453 | 5113 |
| 99 | 8,517 | 25,349 | Republican | 8517 | 0 | 0 | 8416 | 8517 | 8416 | 102 |
| TOTALS | 1,448,901 | 1,394,018 |  | 726,238 | 402,334 | 160,165 | 132,723 | 886,403 | 535,057 | 351,346 |

## D. Conclusions

In this report, I have outlined a method that generates accurate estimates of underlying partisanship using the 2012 presidential election vote, demographics, incumbency, and geographic features to explain patterns of voting in Assembly elections. This method is accurate, as demonstrated by its ability to forecast vote totals at both the individual ward and district levels, and I demonstrate that it generates valid out of sample estimates. It produces results that are very similar to those derived by the expert witness retained by the state legislature during its development of the redistricting map implemented in Act 43.

The results demonstrate that Act 43 was an egregious gerrymander, packing Democratic voters into a small number of districts and distributing Republican voters efficiently in a large number of districts in which they constituted safe majorities. As I demonstrated with the treatment of the city of Sheboygan in Act 43, areas of Democratic strength large enough to constitute majorities in single districts were unnecessarily split and then combined with larger Republican populations to create additional Republican districts and eliminate Democratic districts. The city, which had been in a single Democratic Assembly district since 1992, was split into two Republican districts. This packing and cracking was so successful that Republicans won $61 \%$ of Assembly seats in 2012, while obtaining only $46.5 \%$ of the statewide presidential vote.

The scope of the gerrymander is demonstrated by the efficiency gap calculation for Act 43: $11.69 \%$. Based on the baseline partisanship estimates produced by Dr. Ronald Keith Gaddie during the drawing of the Act 43 plan, this was the intended outcome: using Gaddie's baseline estimates, Act 43 had an expected efficiency gap of $12.36 \%$.

However, I drew a demonstration districting plan that was equivalent to Act 43 on population deviation, municipal splits, and compliance with the Voting Rights Act, and better on compactness, with a dramatically lower efficiency gap score of $2.20 \%$. This proves that Act 43 's extreme partisan effects were not required by these constitutional or statutory mandates.

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## I. Data Issues

The largest errors in the Legislative Technology Services Bureau (LTSB) data occurred because the two data sets used to create this data do not precisely overlap. In GIS argot, the two sets of data are not reported in the same geography. The LTSB files contained data at the individual ward level, while the official election data is aggregated by reporting unit. Wisconsin elections are administered at the ward level, but are often tabulated and released in reporting units consisting of multiple wards. ${ }^{1}$ Of Wisconsin's roughly 6,530 populated wards, only about a third report election results at the individual ward level; the rest report results by combining wards into reporting units. As one example, the city of Manitowoc (2010 population 33,736) has 25 wards, but reports election results in 10 reporting units of between 2 and 6 wards each. ${ }^{2}$

In order to generate data at the ward level, my understanding is that the LTSB disaggregated reporting unit results to individual wards based on the fraction of Voting Age Population in each ward comprising the reporting unit. In the process a number of anomalies crept into the data. The LTSB file for 2012 contains wards where the number of votes cast exceeds the voting age population; wards with large voting age populations and an unusually low number of votes, often zero, recorded; wards, municipalities, and districts with vote totals that differ substantially from what the Government Accountability Board (GAB) reports; votes allocated to the wrong district; incorrectly numbered and duplicated wards; and wards in uncontested Assembly districts with votes recorded for both political parties.

[^14]In most cases, correcting the errors in the LTSB data involved manually changing the incorrect ward totals to reflect GAB results. When the GAB data were combined into reporting units, I allocated votes to each ward in the unit based on the ward's share of the voting eligible population, removing noncitizen and prison populations. ${ }^{3}$ This process generated more accurate ward level data, and is a standard technique when allocating votes into different geographic levels (McDonald 2014; Pavia and López-Quílez 2013). At times, however, the LTSB and GAB data could not be reconciled, because of wards that appeared in one file but not in the other, or discrepancies in ward geography. The votes I was not able to allocate constituted only $0.21 \%$ of the total votes cast in the 2012 Assembly election, and have no effect on any subsequent analysis or my conclusions.

The following table shows some of the problems with the data recorded by the LTSB. It displays the errors in the LTSB 2012 presidential vote totals for the city of Mequon. The GAB Reports columns show the vote totals for each of the city's reporting units taken from the 2014 Wisconsin Blue Book, which I take to be authoritative. ${ }^{4}$ The LTSB Data columns show the results of combining the individual ward data in the LTSB ward file into the GAB reporting units. The Difference columns show the errors in the LTSB data. While the vote totals for the municipality are the same in both data sets, every ward total is different.

[^15]

| GAB Reports |  |  |  | LTSB Data |  |  | Difference |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Reporting Unit (wards) | Obama Votes | Romney Votes | Total Votes | Obama Votes | Romney Votes | Total Votes | Obama Votes | Romney Votes | Total Votes |
| 1 | 534 | 890 | 1424 | 849 | 1,522 | 2,371 | 315 | 632 | 947 |
| 2 | 120 | 391 | 511 | 240 | 633 | 873 | 120 | 242 | 362 |
| 3,4 | 637 | 1,249 | 1886 | 415 | 833 | 1,248 | (222) | (416) | (638) |
| 5, 7B | 205 | 603 | 808 | 155 | 311 | 466 | (50) | (292) | (342) |
| 6, 7A | 392 | 909 | 1301 | 292 | 589 | 881 | (100) | (320) | (420) |
| 8,9,10 | 737 | 1,245 | 1982 | 477 | 956 | 1,433 | (260) | (289) | (549) |
| 11, 12 | 635 | 1,126 | 1761 | 527 | 1,057 | 1,584 | (108) | (69) | (177) |
| 13, 14 | 353 | 770 | 1123 | 253 | 506 | 759 | (100) | (264) | (364) |
| 15 | 380 | 494 | 874 | 579 | 896 | 1,475 | 199 | 402 | 601 |
| 16 | 221 | 491 | 712 | 357 | 766 | 1,123 | 136 | 275 | 411 |
| 17 | 336 | 459 | 795 | 517 | 824 | 1,341 | 181 | 365 | 546 |
| 18 | 204 | 368 | 572 | 322 | 607 | 929 | 118 | 239 | 357 |
| 19,20,21 | 639 | 1,331 | 1970 | 410 | 826 | 1,236 | (229) | (505) | (734) |
| Totals | 5,393 | 10,326 | 15,719 | 5,393 | 10,326 | 15,719 | 0 | 0 | 0 |

Correcting these totals required manually changing the single-ward vote counts to match the GAB data, and allocating votes in reporting units to the individual wards based on the votingeligible population in each ward in the unit (in the following table, wards in a reporting unit are framed together):

Allocation of Reporting Unit Data to Ward Data
City of Mequon, 2012 Presidential Vote

| GAB Data |  |  |  |  | Data Used in Voting Model |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Ward | Obama Votes | Romney Votes | Ward Voting Eligible Population | Ward Share of Reporting Unit VEP | Obama Votes | Romney Votes | Total <br> Votes |
| 1 | 534 | 890 | - | - | 534 | 890 | 1,424 |
| 2 | 120 | 391 | - | - | 120 | 391 | 511 |
| 3 | 637 | 1249 | 1063 | 53\% | 336 | 658 | 994 |
| 4 |  |  | 954 | 47\% | 301 | 591 | 892 |
| 5 | 205 | 603 | 501 | 67\% | 137 | 402 | 539 |
| 7B |  |  | 250 | 33\% | 68 | 201 | 269 |
| 6 | 392 | 909 | 1240 | 87\% | 343 | 794 | 1,137 |
| 7A |  |  | 179 | 13\% | 49 | 115 | 164 |
| 8 | 737 | 1245 | 599 | 26\% | 192 | 324 | 516 |
| 9 |  |  | 457 | 20\% | 146 | 247 | 393 |
| 10 |  |  | 1247 | 54\% | 399 | 674 | 1,073 |
| 11 | 635 | 1126 | 1530 | 60\% | 380 | 673 | 1,053 |
| 12 |  |  | 1029 | 40\% | 255 | 453 | 708 |
| 13 | 353 | 770 | 761 | 63\% | 221 | 482 | 703 |
| 14 |  |  | 455 | 37\% | 132 | 288 | 420 |
| 15 | 380 | 494 | - | - | 380 | 494 | 874 |
| 16 | 221 | 491 | - | - | 221 | 491 | 712 |
| 17 | 336 | 459 | - | - | 336 | 459 | 795 |
| 18 | 204 | 368 | - | - | 204 | 368 | 572 |
| 19 | 639 | 1331 | 908 | 46\% | 291 | 606 | 897 |
| 20 |  |  | 776 | 39\% | 249 | 518 | 767 |
| 21 |  |  | 310 | 16\% | 99 | 207 | 306 |
| Totals | 5,393 | 10,326 |  |  | 5,393 | 10,326 | 15,719 |

I repeated this process for every instance of inaccurate vote totals in the LTSB, using
GAB data as the reference.

## II. Full Regression Results

Republican vote totals (bold variables have $\mathrm{p}<.05$ )

Independent Variable: Assembly Republican Votes
$\left.\begin{array}{|r|c|c|c|c|}\hline \begin{array}{l}\text { Dependent } \\ \text { Variable }\end{array} & \text { Coefficient } & \begin{array}{c}\text { Robust } \\ \text { Std. Error }\end{array} & \text { t-statistic } & \text { P-value } \\ \hline \begin{array}{r}\text { Total Voting } \\ \text { Eligible }\end{array} & 0.01 & & & \\ \text { Population }\end{array}\right)$

| Columbia | 15.01 | 10.08 | 1.49 | 0.141 |
| :---: | :---: | :---: | :---: | :---: |
| Crawford | 28.20 | 7.24 | 3.90 | 0 |
| Dane | 1.55 | 8.53 | 0.18 | 0.857 |
| Dodge | 8.54 | 7.88 | 1.08 | 0.282 |
| Door | 16.98 | 7.23 | 2.35 | 0.022 |
| Douglas | -3.14 | 7.65 | -0.41 | 0.682 |
| EauClaire | 0.47 | 7.83 | 0.06 | 0.953 |
| Florence | -7.34 | 7.52 | -0.98 | 0.332 |
| FondduLac | 4.74 | 8.07 | 0.59 | 0.559 |
| Forest | -1.91 | 7.39 | -0.26 | 0.796 |
| Grant | 24.64 | 7.23 | 3.41 | 0.001 |
| Green | 14.41 | 9.95 | 1.45 | 0.152 |
| GreenLake | 11.96 | 7.36 | 1.62 | 0.109 |
| lowa | 15.04 | 8.08 | 1.86 | 0.067 |
| Iron | 20.54 | 7.68 | 2.67 | 0.009 |
| Jackson | 5.74 | 7.53 | 0.76 | 0.449 |
| Jefferson | 2.37 | 8.41 | 0.28 | 0.779 |
| Juneau | -4.31 | 7.29 | -0.59 | 0.556 |
| Kenosha | 3.73 | 7.99 | 0.47 | 0.642 |
| Kewaunee | -14.13 | 7.24 | -1.95 | 0.055 |
| LaCrosse | -26.58 | 8.43 | -3.15 | 0.002 |
| Lafayette | 18.18 | 7.29 | 2.49 | 0.015 |
| Langlade | 4.35 | 8.30 | 0.52 | 0.602 |
| Lincoln | -0.38 | 7.53 | -0.05 | 0.96 |
| Manitowoc | 19.35 | 9.36 | 2.07 | 0.042 |
| Marathon | 2.01 | 8.56 | 0.24 | 0.815 |
| Marinette | 19.89 | 8.04 | 2.48 | 0.016 |
| Marquette | 6.91 | 7.26 | 0.95 | 0.344 |
| Menominee | -3.08 | 7.32 | -0.42 | 0.675 |
| Milwaukee | 1.96 | 11.98 | 0.16 | 0.871 |
| Monroe | 19.47 | 7.72 | 2.52 | 0.014 |
| Oconto | 3.21 | 7.95 | 0.40 | 0.687 |
| Oneida | 12.01 | 7.95 | 1.51 | 0.136 |
| Outagamie | 1.90 | 8.02 | 0.24 | 0.814 |
| Ozaukee | 13.71 | 8.82 | 1.55 | 0.125 |
| Pepin | -9.83 | 7.27 | -1.35 | 0.181 |
| Pierce | -9.31 | 7.18 | -1.30 | 0.199 |
| Polk | -3.47 | 7.24 | -0.48 | 0.633 |
| Portage | -20.74 | 7.71 | -2.69 | 0.009 |
| Price | 5.25 | 7.75 | 0.68 | 0.501 |
| Racine | -6.90 | 8.23 | -0.84 | 0.404 |
| Richland | 16.24 | 8.55 | 1.90 | 0.062 |
| Rock | 9.24 | 8.32 | 1.11 | 0.27 |


| Rusk | 3.71 | 7.37 | 0.50 | 0.616 |
| :---: | :---: | :---: | :---: | :---: |
| SaintCroix | 13.80 | 9.31 | 1.48 | 0.143 |
| Sauk | $\mathbf{1 6 . 6 8}$ | $\mathbf{8 . 2 7}$ | $\mathbf{2 . 0 2}$ | $\mathbf{0 . 0 4 8}$ |
| Sawyer | -0.90 | 7.40 | -0.12 | 0.903 |
| Shawano | 2.70 | 7.86 | 0.34 | 0.733 |
| Sheboygan | -6.50 | 15.54 | -0.42 | 0.677 |
| Taylor | 9.96 | 7.30 | 1.37 | 0.176 |
| Trempealeau | 1.29 | 7.21 | 0.18 | 0.859 |
| Vernon | $\mathbf{3 1 . 5 4}$ | $\mathbf{7 . 2 9}$ | $\mathbf{4 . 3 3}$ | $\mathbf{0}$ |
| Vilas | 3.61 | 7.64 | 0.47 | 0.638 |
| Walworth | -2.00 | 8.17 | -0.24 | 0.807 |
| Washburn | -10.80 | 7.31 | -1.48 | 0.144 |
| Washington | 14.16 | 12.70 | 1.12 | 0.269 |
| Waukesha | 1.18 | 7.93 | 0.15 | 0.882 |
| Waupaca | -8.08 | 7.26 | -1.11 | 0.27 |
| Waushara | -3.47 | 7.30 | -0.48 | 0.636 |
| Winnebago | 30.00 | 17.09 | 1.76 | 0.084 |
| Wood | -7.60 | 8.96 | -0.85 | 0.399 |
| Constant | -0.92 | 7.52 | -0.12 | 0.903 |


| N | 5282.00 |
| :---: | :---: |
| R-squared | 0.9903 |
| Root MSE | 15.823 |

Democratic vote totals

Independent Variable: Assembly Democratic Votes

| Dependent Variable | Coefficient | Robust <br> Std. Error | t-statistic | P-value |
| :---: | :---: | :---: | :---: | :---: |
| Total Voting Eligible Population | -0.01 | 0.01 | -0.65 | 0.52 |
| Black Voting Eligible Population | -0.02 | 0.04 | -0.49 | 0.63 |
| Hispanic Voting Eligible Population | -0.15 | 0.05 | -3.01 | 0.00 |
| Democratic <br> Presidential <br> Votes | 0.93 | 0.03 | 33.33 | 0.00 |
| Republican <br> Presidential <br> Votes | 0.01 | 0.01 | 0.98 | 0.33 |
| Democratic Assembly Incumbent | 0.03 | 0.01 | 3.85 | 0.00 |
| Republican Assembly Incumbent | -0.01 | 0.01 | -2.77 | 0.01 |
| Adams | -14.45 | 6.73 | -2.15 | 0.04 |
| Ashland | -4.78 | 5.58 | -0.86 | 0.40 |
| Barron | 14.57 | 4.04 | 3.60 | 0.00 |
| Bayfield | -2.82 | 5.58 | -0.50 | 0.62 |
| Brown | -21.57 | 7.80 | -2.77 | 0.01 |
| Buffalo | 5.10 | 4.86 | 1.05 | 0.30 |
| Burnett | -3.84 | 4.69 | -0.82 | 0.42 |
| Calumet | -26.32 | 5.81 | -4.53 | 0.00 |
| Chippewa | 0.98 | 9.53 | 0.10 | 0.92 |
| Clark | -6.83 | 4.80 | -1.42 | 0.16 |
| Columbia | -19.51 | 8.15 | -2.39 | 0.02 |
| Crawford | -32.57 | 4.33 | -7.51 | 0.00 |
| Dane | -9.39 | 7.20 | -1.31 | 0.20 |
| Dodge | -8.49 | 5.27 | -1.61 | 0.11 |
| Door | -11.92 | 4.51 | -2.64 | 0.01 |
| Douglas | -7.18 | 5.40 | -1.33 | 0.19 |
| EauClaire | 1.05 | 7.22 | 0.14 | 0.89 |
| Florence | -13.53 | 5.33 | -2.54 | 0.01 |
| FondduLac | -25.18 | 4.92 | -5.12 | 0.00 |
| Forest | -10.83 | 6.06 | -1.79 | 0.08 |

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| Grant | -23.14 | 4.26 | -5.43 | 0.00 |
| :---: | :---: | :---: | :---: | :---: |
| Green | -15.68 | 6.63 | -2.36 | 0.02 |
| GreenLake | -17.01 | 4.65 | -3.66 | 0.00 |
| Iowa | -19.48 | 4.91 | -3.96 | 0.00 |
| Iron | -30.91 | 5.54 | -5.58 | 0.00 |
| Jackson | -12.37 | 6.44 | -1.92 | 0.06 |
| Jefferson | -17.18 | 7.09 | -2.42 | 0.02 |
| Juneau | -5.78 | 4.55 | -1.27 | 0.21 |
| Kenosha | 1.78 | 5.33 | 0.33 | 0.74 |
| Kewaunee | 17.69 | 4.41 | 4.01 | 0.00 |
| LaCrosse | 25.17 | 6.69 | 3.76 | 0.00 |
| Lafayette | -22.66 | 4.58 | -4.95 | 0.00 |
| Langlade | -22.20 | 6.05 | -3.67 | 0.00 |
| Lincoln | -13.42 | 5.15 | -2.61 | 0.01 |
| Manitowoc | -15.90 | 5.49 | -2.90 | 0.01 |
| Marathon | -5.64 | 6.20 | -0.91 | 0.37 |
| Marinette | -26.28 | 4.22 | -6.23 | 0.00 |
| Marquette | -15.87 | 4.48 | -3.54 | 0.00 |
| Menominee | -61.44 | 4.41 | -13.95 | 0.00 |
| Milwaukee | -29.20 | 6.47 | -4.51 | 0.00 |
| Monroe | -26.83 | 5.44 | -4.93 | 0.00 |
| Oconto | -12.99 | 4.42 | -2.94 | 0.00 |
| Oneida | -35.94 | 5.19 | -6.92 | 0.00 |
| Outagamie | -14.60 | 6.94 | -2.10 | 0.04 |
| Ozaukee | -17.19 | 5.83 | -2.95 | 0.00 |
| Pepin | 6.62 | 4.52 | 1.46 | 0.15 |
| Pierce | 12.49 | 4.00 | 3.12 | 0.00 |
| Polk | 5.81 | 4.32 | 1.35 | 0.18 |
| Portage | -0.04 | 5.13 | -0.01 | 0.99 |
| Price | -14.62 | 5.64 | -2.59 | 0.01 |
| Racine | 4.42 | 5.29 | 0.83 | 0.41 |
| Richland | -26.22 | 5.30 | -4.95 | 0.00 |
| Rock | -4.48 | 8.87 | -0.50 | 0.62 |
| Rusk | -8.01 | 4.90 | -1.64 | 0.11 |
| SaintCroix | -6.89 | 6.67 | -1.03 | 0.31 |
| Sauk | -19.42 | 6.51 | -2.98 | 0.00 |
| Sawyer | -6.06 | 4.64 | -1.30 | 0.20 |
| Shawano | -14.93 | 4.58 | -3.26 | 0.00 |
| Sheboygan | 15.96 | 17.17 | 0.93 | 0.36 |
| Taylor | -6.81 | 4.56 | -1.49 | 0.14 |
| Trempealeau | -3.89 | 4.29 | -0.91 | 0.37 |
| Vernon | -32.42 | 4.52 | -7.18 | 0.00 |
| Vilas | -27.14 | 5.48 | -4.95 | 0.00 |

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| Walworth | 0.34 | 5.26 | 0.07 | 0.95 |
| :--- | :---: | :---: | :---: | :---: |
| Washburn | 6.43 | 4.74 | 1.36 | 0.18 |
| Washington | $\mathbf{- 1 9 . 2 3}$ | $\mathbf{9 . 7 5}$ | $\mathbf{- 1 . 9 7}$ | $\mathbf{0 . 0 5}$ |
| Waukesha | $\mathbf{- 1 7 . 6 3}$ | $\mathbf{5 . 5 5}$ | $\mathbf{- 3 . 1 8}$ | $\mathbf{0 . 0 0}$ |
| Waupaca | $\mathbf{- 1 0 . 4 8}$ | $\mathbf{4 . 3 7}$ | $\mathbf{- 2 . 4 0}$ | $\mathbf{0 . 0 2}$ |
| Waushara | 0.21 | 4.64 | 0.04 | 0.97 |
| Winnebago | $\mathbf{- 3 2 . 1 2}$ | $\mathbf{1 5 . 9 4}$ | $\mathbf{- 2 . 0 2}$ | $\mathbf{0 . 0 5}$ |
| Wood | 8.14 | 6.01 | 1.35 | 0.18 |
| Constant | 9.80 | 5.39 | 1.82 | 0.07 |
| $\quad$ |  |  |  |  |
| N | 5282.00 |  |  |  |
| R-squared | 0.9843 |  |  |  |
| Root MSE | 17.675 |  |  |  |

## III. Plan characteristics

A. Population deviation

| Assembly <br> District | Population | Deviation <br> from <br> Ideal | $\%$ <br> Deviation |
| :---: | ---: | ---: | ---: |
| 1 | 57,487 | 43 | $0.07 \%$ |
| 2 | 57,590 | 146 | $0.25 \%$ |
| 3 | 57,686 | 242 | $0.42 \%$ |
| 4 | 57,406 | -38 | $-0.07 \%$ |
| 5 | 57,633 | 189 | $0.33 \%$ |
| 6 | 57,480 | 36 | $0.06 \%$ |
| 7 | 57,208 | -236 | $-0.41 \%$ |
| 8 | 57,196 | -248 | $-0.43 \%$ |
| 9 | 57,420 | -24 | $-0.04 \%$ |
| 10 | 57,195 | -249 | $-0.43 \%$ |
| 11 | 57,455 | 11 | $0.02 \%$ |
| 12 | 57,420 | -24 | $-0.04 \%$ |
| 13 | 57,248 | -196 | $-0.34 \%$ |
| 14 | 57,333 | -111 | $-0.19 \%$ |
| 15 | 57,514 | 70 | $0.12 \%$ |
| 16 | 57,282 | -162 | $-0.28 \%$ |
| 34 | 57,437 | -7 | $-0.01 \%$ |
| 35 | 57,528 | 84 | $0.15 \%$ |
| 36 | 57,377 | -67 | $-0.12 \%$ |


| 37 | 57,671 | 227 | 0.40\% |
| :---: | :---: | :---: | :---: |
| 38 | 57,572 | 128 | 0.22\% |
| 39 | 57,457 | 13 | 0.02\% |
| 40 | 57,495 | 51 | 0.09\% |
| 41 | 57,671 | 227 | 0.40\% |
| 42 | 57,559 | 115 | 0.20\% |
| 43 | 57,444 | 0 | 0.00\% |
| 44 | 57,434 | -10 | -0.02\% |
| 45 | 57,242 | -202 | -0.35\% |
| 46 | 57,463 | 19 | 0.03\% |
| 47 | 57,494 | 50 | 0.09\% |
| 48 | 57,568 | 124 | 0.22\% |
| 49 | 57,389 | -55 | -0.10\% |
| 50 | 57,465 | 21 | 0.04\% |
| 51 | 57,247 | -197 | -0.34\% |
| 52 | 57,384 | -60 | -0.10\% |
| 53 | 57,444 | 0 | 0.00\% |
| 54 | 57,443 | -1 | 0.00\% |
| 55 | 57,446 | 2 | 0.00\% |
| 56 | 57,342 | -102 | -0.18\% |
| 57 | 57,404 | -40 | -0.07\% |
| 58 | 57,436 | -8 | -0.01\% |
| 59 | 57,554 | 110 | 0.19\% |
| 60 | 57,547 | 103 | 0.18\% |
| 61 | 57,605 | 161 | 0.28\% |
| 62 | 57,632 | 188 | 0.33\% |
| 63 | 57,299 | -145 | -0.25\% |
| 64 | 57,266 | -178 | -0.31\% |
| 65 | 57,601 | 157 | 0.27\% |
| 66 | 57,459 | 15 | 0.03\% |
| 67 | 57,378 | -66 | -0.11\% |
| 68 | 57,254 | -190 | -0.33\% |
| 69 | 57,424 | -20 | -0.03\% |
| 70 | 57,415 | -29 | -0.05\% |
| 71 | 57,228 | -216 | -0.38\% |
| 72 | 57,654 | 210 | 0.37\% |
| 73 | 57,491 | 47 | 0.08\% |
| 74 | 57,320 | -124 | -0.22\% |
| 75 | 57,255 | -189 | -0.33\% |
| 76 | 57,586 | 142 | 0.25\% |
| 77 | 57,398 | -46 | -0.08\% |
| 78 | 57,579 | 135 | 0.24\% |
| 79 | 57,341 | -103 | -0.18\% |


| 80 | 57,385 | -59 | $-0.10 \%$ |
| :--- | ---: | ---: | ---: |
| 81 | 57,266 | -178 | $-0.31 \%$ |
| 82 | 57,641 | 197 | $0.34 \%$ |
| 83 | 57,612 | 168 | $0.29 \%$ |
| 84 | 57,375 | -69 | $-0.12 \%$ |
| 85 | 57,529 | 85 | $0.15 \%$ |
| 86 | 57,477 | 33 | $0.06 \%$ |
| 87 | 57,661 | 217 | $0.38 \%$ |
| 88 | 57,533 | 89 | $0.15 \%$ |
| 89 | 57,490 | 46 | $0.08 \%$ |
| 90 | 57,617 | 173 | $0.30 \%$ |
| 91 | 57,374 | -70 | $-0.12 \%$ |
| 92 | 57,421 | -23 | $-0.04 \%$ |
| 93 | 57,280 | -164 | $-0.29 \%$ |
| 94 | 57,509 | 65 | $0.11 \%$ |
| 95 | 57,496 | 52 | $0.09 \%$ |
| 96 | 57,406 | -38 | $-0.07 \%$ |
| 97 | 57,487 | 43 | $0.07 \%$ |
| 98 | 57,485 | 41 | $0.07 \%$ |
| 99 | 57,657 | 213 | $0.37 \%$ |

B. Compactness (Reock or smallest circle measure)

| Assembly <br> District | Smallest <br> Circle <br> Measure |
| :---: | :---: |
| 1 | 0.44 |
| 2 | 0.46 |
| 3 | 0.42 |
| 4 | 0.55 |
| 5 | 0.39 |
| 6 | 0.35 |
| 7 | 0.52 |
| 8 | 0.66 |
| 9 | 0.39 |
| 10 | 0.45 |
| 11 | 0.39 |
| 12 | 0.36 |
| 13 | 0.28 |
| 14 | 0.44 |
| 15 | 0.49 |
| 16 | 0.52 |
| 17 | 0.52 |

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| 18 | 0.30 |
| :---: | :---: |
| 19 | 0.30 |
| 20 | 0.44 |
| 21 | 0.40 |
| 22 | 0.34 |
| 23 | 0.42 |
| 24 | 0.42 |
| 25 | 0.57 |
| 26 | 0.49 |
| 27 | 0.53 |
| 28 | 0.31 |
| 29 | 0.49 |
| 30 | 0.50 |
| 31 | 0.60 |
| 32 | 0.45 |
| 33 | 0.30 |
| 34 | 0.42 |
| 35 | 0.49 |
| 36 | 0.43 |
| 37 | 0.34 |
| 38 | 0.24 |
| 39 | 0.30 |
| 40 | 0.51 |
| 41 | 0.39 |
| 42 | 0.33 |
| 43 | 0.29 |
| 44 | 0.43 |
| 45 | 0.37 |
| 46 | 0.35 |
| 47 | 0.26 |
| 48 | 0.43 |
| 49 | 0.35 |
| 50 | 0.44 |
| 51 | 0.53 |
| 52 | 0.56 |
| 53 | 0.27 |
| 54 | 0.28 |
| 55 | 0.37 |
| 56 | 0.57 |
| 57 | 0.26 |
| 58 | 0.40 |
| 59 | 0.37 |
| 60 | 0.55 |

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| 61 | 0.39 |
| :--- | :--- |
| 62 | 0.25 |
| 63 | 0.43 |
| 64 | 0.27 |
| 65 | 0.32 |
| 66 | 0.32 |
| 67 | 0.56 |
| 68 | 0.52 |
| 69 | 0.31 |
| 70 | 0.28 |
| 71 | 0.34 |
| 72 | 0.35 |
| 73 | 0.28 |
| 74 | 0.37 |
| 75 | 0.36 |
| 76 | 0.23 |
| 77 | 0.39 |
| 78 | 0.51 |
| 79 | 0.59 |
| 80 | 0.33 |
| 81 | 0.55 |
| 82 | 0.37 |
| 83 | 0.26 |
| 84 | 0.28 |
| 85 | 0.58 |
| 86 | 0.36 |
| 87 | 0.35 |
| 88 | 0.35 |
| 89 | 0.56 |
| 90 | 0.52 |
| 91 | 0.49 |
| 92 | 0.49 |
| 93 | 0.42 |
| 94 | 0.44 |
| 95 | 0.42 |
| 96 | 0.39 |
| 97 | 0.32 |
| 98 | 0.41 |
| 99 | 0.30 |
|  |  |


[^0]:    ${ }^{1}$ The federal requirements are equal population, compliance with Section 2 of the Voting Rights Act, and the ban on racially gerrymandered districts. The state requirements are contiguity, compactness, and respect for political subdivisions (counties, towns, cities, and villages).

[^1]:    ${ }^{2}$ Winners are determined by which candidate receives $>50 \%$ of the vote in a two party race. Seats votes curves depend on the number of seats a party wins in an election (determined by the number of races in which that party received $>50 \%$ of the vote) and the statewide vote totals in legislative races or some other set of statewide races

[^2]:    ${ }^{3}$ Legislative Technology Services Bureau data show 6,592 wards in Wisconsin, of which 66 are unpopulated and another 50 have fewer than 10 people. The average populated ward contains 869 people. Wisconsin statutes 5.15 (2)(b) specifies a permissible population range for wards of 300-4,000, depending on a municipality's size, with exceptions allowed in certain circumstances (for example, when single blocks exceed a permitted ward size, or when a municipality is divided into multiple counties or school districts, contains islands, or has wards that must be altered to match district boundaries).

[^3]:    ${ }^{4}$ The larger n also means that OLS is an accurate method of estimating the underlying relationships, whereas more complicated techniques may be required with smaller sample sizes (Afshartous and de Leeuw 2005).
    ${ }^{5}$ The Census Bureau uses the term "Voting Tabulation District" (VTD). Most states call VTDs precincts. In Wisconsin these units are called "wards."
    ${ }^{6}$ These are known as FIPS (Federal Information Processing Standard) codes. http://www.census.gov/geo/reference/ansi.html.

[^4]:    ${ }^{7}$ The files are available at http://legis.wisconsin.gov/gis/data. The 2012 election results are in the file Wards_111312_ED_110612.xlsx.
    ${ }^{8}$ As I note in the Annex, I was not able to allocate $0.21 \%$ of the vote in 2012 because of inconsistencies between electoral data reported by the GAB and the geographic redistricting data reported by the LTSB. This small number of votes will not change any of my analysis or conclusions, and such errors are inevitable when working with large data sets.

[^5]:    ${ }^{9}$ When using dummy variables (which take binary values of either 0 or 1 ) to measure effects in units or conditions across the full population, one unit must be excluded, as otherwise perfect collinearity prevents estimation (Greene 1990, 240-241).

[^6]:    ${ }^{10}$ The reliance on actual numbers of voters eliminates the Modified Areal Unit Problem, which results when group statistics such as vote percentages or demographic fractions are aggregated into different geographic units levels. All of my variables and measures are scale invariant (see King 1996).
    ${ }^{11}$ The number of votes cast in Assembly races varies considerably even in in contested races. In 2012, the number of major party votes cast in the highest turnout Assembly election in the $23^{\text {rd }}$ Assembly district, 36,205 , was almost twice the number cast in the $90^{\text {th }}$ Assembly district, 18,735 , and almost 5 times the number cast in the uncontested $8^{\text {th }}$ district, 7,869 (numbers taken from GAB figures).
    ${ }^{12}$ The voting eligible population (VEP) adjusts the voting age population by removing adults who are not eligible to vote. In Wisconsin, the two largest categories of ineligible adults that can be identified geographically are noncitizens and adults in prison for felonies. Noncitizens were removed using the 2008-2012 5 year American Community Survey county level noncitizen estimates (available at http://www.census.gov/acs/www/data_documentation/2012_release/. Institutionalized prison populations were identified using Census Bureau "Advanced Group Quarters" files for Wisconsin, available at .http://www2.census.gov/census_2010/02Advance Group Quarters/, and described in http://www.census.gov/newsroom/releases/archives/2010_census/cb11-tps13.html. There are individuals on probation or extended supervision who are also ineligible to vote. I was not able to systematically identify their locations, but they are dispersed enough that they will not have a material effect on my resulting estimates or conclusions. All regression results and district estimates are materially unchanged when the unadjusted data are used.

[^7]:    ${ }^{13}$ In the political science literature, the incumbency advantage has been attributed to the political skills and campaign experience of officeholders, higher name recognition, fundraising advantages, constituency service, redistricting, and the ability to scare off quality challengers. ${ }^{14}$ Incumbents were identified using 2012 election data in the 2013 Wisconsin Blue Book. In the $43^{\text {rd }}$ and $61^{\text {st }}$ Assembly districts two incumbents were paired against each other; these districts were coded as having no incumbent, since the advantage cancels. In the $7^{\text {th }}$ Assembly district, the Democratic incumbent lost in the primary election and ran a write in campaign in the general election. Because the incumbent was not on the ballot, this district is also coded as having no incumbent.

[^8]:    ${ }^{15}$ This major-party contested definition is standard. It counts as uncontested four districts where one major party candidate was not on the ballot but received votes as a write in (districts 7, 17, 48, and 57), and one district (district 95) where one major party candidate was on the ballot but did not campaign and received only 50 votes (or $0.24 \%$ ). This is consistent with methods used in the literature, which often uses a $95 \%$ threshold for the winning candidate as a standard (Gelman and King 1990, 274).
    ${ }^{16}$ Standard errors were adjusted to reflect the aggregation (or clustering) of wards into districts. The full set of variables is included in an appendix to this report.

[^9]:    ${ }^{17}$ All of the votes for a losing candidate are defined as wasted, whereas only those votes in excess of the number required to win are wasted for the winner.
    ${ }^{18}$ The vote percentages were calculated using the actual and predicted vote totals.

[^10]:    ${ }^{19}$ Uncontested districts were not included in the analysis for reasons specified in section B(1)(f) above.
    ${ }^{20}$ In twelve districts (districts $1,6,34,35,36,49,68,74,75,93,94$ and 96 ), at least one county was entirely contained in a single district, making it impossible to estimate the fixed effect coefficient value for that county. Consequently, when the out-of-sample predictions were calculated, a variable was missing. An accurate test involves districts for which it was possible to estimate the full model.

[^11]:    ${ }^{21}$ Deposition, January 20, 2012, p. 196.
    ${ }^{22}$ I generated this data by calculating predicted values for my model in Act 43 districts, setting all incumbency variables to zero.

[^12]:    ${ }^{23}$ The identifier is a combination of state, county, Census tract, and block FIPS codes.

[^13]:    ${ }^{24}$ Act 43 figures are taken from the Joint Final Pretrial Report filed in Baldus et al. vs Brennan et al.11-CV-562, filed February 24, 2012.

[^14]:    ${ }^{1}$ Wisconsin Statutes $5.15(6)(\mathrm{b})$ allows municipalities with a population under 35,000 to combine wards for purposes of using a common polling place, and allows for the tabulation and reporting of combined ward vote totals.
    ${ }^{2}$ In 2012 the reporting units were Wards $1-2 ; 5-6 ; 7-8 ; 9-10 ; 11-12 ; 13-14 ; 15-16 ; 3,4$, and 22; and 17-18, 21, and 23-25.

[^15]:    ${ }^{3}$ The voting eligible population (VEP) adjusts the voting age population by removing adults who are not eligible to vote. In Wisconsin, the two largest categories of ineligible adults are noncitizens and adults in prison for felonies. Noncitizens were removed using the 2008-2012 5 year American Community Survey county level noncitizen estimates (available at http://www.census.gov/acs/www/data_documentation/2012_release/. Institutionalized prison populations were identified and removed using Census Bureau "Advanced Group Quarters" files for Wisconsin, available at http://www2.census.gov/census_2010/02-Advance_Group_Quarters/, and described in http://www.census.gov/newsroom/releases/archives/2010_census/cb11tps13.html.
    ${ }^{4}$ Table: Vote for President and Vice President by Ward, November 6, 2012 General Election, 938.

